

Package ‘pcgen’

February 18, 2019

Type Package

Title Reconstruction of Causal Networks for Data with Random Genetic Effects

Version 0.2.0

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Depends R (>= 3.1.0)

Imports pcalg, graph, Matrix, stats, MASS, utils, Hmisc, methods, lme4, sommer, ggm

Description

Implements the pcgen algorithm, which is a modified version of the standard pc-algorithm, with specific conditional independence tests and modified orientation rules. pcgen extends the approach of Valente et al. (2010) <doi:10.1534/genetics.109.112979> with reconstruction of direct genetic effects.

License GPL-3

Date 2019-02-18

NeedsCompilation no

Repository CRAN

Date/Publication 2019-02-18 14:50:03 UTC

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checkG *Check for consistency in genetic effects*

Description

Given output from `pcgen` or `pcgenFast`, this function checks whether the estimated graph is consistent with the set of traits having significant genetic variance. The function detects traits that have significant genetic variance but for which there is no partially directed path from G.

Usage

```
checkG(pcgen.output, suffStat, alpha = 0.01, covariates = NULL)
```

Arguments

<code>pcgen.output</code>	A graph with nodes G (genotype) and a number of traits. Typically output from <code>pcgen</code> or <code>pcgenFast</code> .
<code>suffStat</code>	A data.frame, of which the first column is the factor G (genotype), and subsequent columns contain the traits, and optionally some QTLs. The name of the first column should be G.
<code>alpha</code>	The significance level used in each conditional independence test. Default is 0.01.
<code>covariates</code>	A data.frame containing covariates, to be used in each conditional independence test. Cannot contain factors. Should be either NULL (default) or a data.frame with the same number of rows as <code>suffStat</code> . An intercept is already included for each trait in <code>suffStat</code> ; covariates should not contain a column of ones.

Value

A logical matrix of dimension $(p + 1) \times (p + 1)$, p being the number of traits. Most entries are FALSE, except those in the first row and column for which there are conflicts. Entries $[1, j]$ and $[j, 1]$ are TRUE if the j th trait has significant genetic variance, but there is no partially directed path from G towards that trait. The matrix can then be used in a subsequent run of `pcgen` or `pcgenFast`, in the `fixedEdges` argument. The arguments `suffStat`, `alpha` and `covariates` should stay the same throughout (first run of `pcgen`, `checkG`, second run of `pcgen`).

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References

Kruijer, W., Behrouzi, P., Rodriguez-Alvarez, M. X., Wit, E. C., Mahmoudi, S. M., Yandell, B., Van Eeuwijk, F., (2018, in preparation), Reconstruction of networks with direct and indirect genetic effects.

gencovTest	<i>Estimate genetic covariances between all pairs of traits, and test their significance</i>
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Description

For each pair of traits in suffStat, we fit a bivariate mixed model, and perform a likelihood ratio test for the null-hypothesis of zero genetic covariance.

Usage

```
gencovTest(suffStat, max.iter = 200, out.cor = TRUE)
```

Arguments

suffStat	A data.frame with (p + 1) columns, of which the first column is the factor G (genotype), and subsequent p columns contain traits. It should not contain covariates or QTLs.
max.iter	Maximum number of iterations in the EM-algorithm, used to fit the bivariate mixed model.
out.cor	If TRUE, the output will contain estimates of genetic correlations; otherwise covariances. The pvalues are always for genetic covariance.

Value

A list with elements pvalues and out.cor, which are both p x p matrices

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References

Kruijer, W., Behrouzi, P., Rodriguez-Alvarez, M. X., Wit, E. C., Mahmoudi, S. M., Yandell, B., Van Eeuwijk, F., (2018, in preparation), Reconstruction of networks with direct and indirect genetic effects.

Examples

```
data(simdata)
test <- gencovTest(suffStat= simdata, max.iter = 200, out.cor= TRUE )
```

getResiduals *Residuals from the GBLUP*

Description

Residuals from the best linear unbiased predictor of the genetic effects (GBLUP), which is computed given REML-estimates of the variance components.

Usage

```
getResiduals(suffStat, covariates = NULL, cov.method = "uni", K = NULL)
```

Arguments

suffStat	A data.frame, of which the first column is the factor G (genotype), and subsequent columns contain the traits. The name of the first column should be G.
covariates	A data.frame containing covariates, that should always be used in each conditional independence test. Should be either NULL (default) or a data.frame with the same number of rows as suffStat. An intercept is already included for each trait in suffStat; covariates should not contain a column of ones.
cov.method	(A string, specifying which method should be used to compute the GBLUP. Options are "us" (unstructured multi-trait model fitted using sommer) and "uni" (based on univariate GBLUPs). Default is "uni").
K	A genetic relatedness matrix. If NULL (default), independent genetic effects are assumed.

Details

If `cov.method = "uni"`, the GBLUP and the residuals are computed separately for each trait in `suffStat`. The covariance of each trait is then assumed to be

$$\sigma_G^2 Z K Z^t + \sigma_E^2 I_n$$

where Z is a binary incidence matrix, assigning plants or plots to genotypes. Z is based on the first column in `suffStat`. If there is a single observation per genotype (typically a genotypic mean), Z is the identity matrix, and the relatedness matrix K should be specified. If there are replicates for at least some of the genotypes, and no K is provided, independent genetic effects are assumed (K will be the identity matrix). It is also possible to have replicates and specify a non-diagonal K . Whenever K is specified, `sommer` (`mmer2`) will be used; otherwise `lmer` (`lme4`). The `mmer2` is also used when `cov.method = "us"`, in which case the multivariate GBLUP is computed, for all traits in `suffStat` simultaneously. This is only possible for a limited number of traits.

Value

A data-frame with the residuals.

Author(s)

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References

Covarrubias-Pazaran, G., 2016. Genome-assisted prediction of quantitative traits using the R package sommer. PloS one, 11(6), p.e0156744.

Examples

```
data(simdata)
rs <- getResiduals(suffStat= simdata)
```

 pcgen

Causal inference with genetic effects

Description

Reconstruction of directed networks with random genetic effects, based on phenotypic observations. The pcgen algorithm is a modification of the pc-stable algorithm of Colombo & Maathuis (2014). It is assumed that there are replicates, and independent genetic effects.

Usage

```
pcgen(suffStat, covariates = NULL, QTLs = integer(), alpha = 0.01, m.max = Inf,
fixedEdges = NULL, fixedGaps = NULL, verbose = FALSE, use.res = FALSE,
res.cor = NULL, max.iter = 50, stop.if.significant = TRUE, return.pvalues = FALSE)
```

Arguments

suffStat	A data.frame, of which the first column is the factor G (genotype), and subsequent columns contain the traits, and optionally some QTLs. The name of the first column should be G. Should not contain covariates.
covariates	A data.frame containing covariates, that should always be used in each conditional independence test. Should be either NULL (default) or a data.frame with the same number of rows as suffStat. An intercept is already included for each trait in suffStat; covariates should not contain a column of ones.
QTLs	Column numbers in suffStat that correspond to QTLs.
alpha	The significance level used in each conditional independence test. Default is 0.01
m.max	Maximum size of the conditioning sets

<code>fixedEdges</code>	A logical matrix of dimension $(p + 1) \times (p + 1)$, where p is the number of traits. The first row and column refer to the node G , and subsequent rows and columns to the traits. As in the <code>pcalg</code> package, the edge $i - j$ is never considered for removal if the entry $[i, j]$ or $[j, i]$ (or both) are TRUE. In that case, the edge is guaranteed to be present in the resulting graph.
<code>fixedGaps</code>	A logical matrix of dimension $(p + 1) \times (p + 1)$, where p is the number of traits. The first row and column refer to the node G , and subsequent rows and columns to the traits. As in the <code>pcalg</code> package, the edge $i - j$ is removed before starting the algorithm if the entry $[i, j]$ or $[j, i]$ (or both) are TRUE. In that case, the edge is guaranteed to be absent in the resulting graph.
<code>verbose</code>	If TRUE, p-values for the conditional independence tests are printed
<code>use.res</code>	If TRUE, the test for conditional independence of 2 traits given a set of other traits and G is based on residuals from GBLUP. If FALSE (the default), it is based on bivariate mixed models.
<code>res.cor</code>	If <code>use.res = TRUE</code> , <code>res.cor</code> should be the correlation matrix of the residuals from the GBLUP. These can be obtained with the <code>getResiduals</code> function. See the example below.
<code>max.iter</code>	Maximum number of iterations in the EM-algorithm, used to fit the bivariate mixed model (when <code>use.res = FALSE</code>).
<code>stop.if.significant</code>	If TRUE, the EM-algorithm used in some of the conditional independence tests (when <code>use.res = FALSE</code>) will be stopped whenever the p-value becomes significant, i.e. below <code>alpha</code> . This will speed up calculations, and can be done because (1) the PC algorithm only needs an accept/reject decision (2) In EM the likelihood is nondecreasing. Should be put to FALSE if the precise p-values are of interest.
<code>return.pvalues</code>	If TRUE, the maximal p-value for each edge is returned.

Details

The `pcgen` function is based on the `pc` function from the `pcalg` package (Kalisch et al. (2012) and Hauser and Buhlmann (2012)).

Value

If `return.pvalues = FALSE`, the output is a graph (an object with S3 class "pcgen"). If `return.pvalues = TRUE`, the output is a list with elements `gr` (the graph) and `pMax` (a matrix with the p-values).

Author(s)

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References

1. Kruijer, W., Behrouzi, P., Rodriguez-Alvarez, M. X., Wit, E. C., Mahmoudi, S. M., Yandell, B., Van Eeuwijk, F., (2018, in preparation), Reconstruction of networks with direct and indirect genetic

effects.

2. Colombo, D. and Maathuis, M.H., 2014. Order-independent constraint-based causal structure learning. *The Journal of Machine Learning Research*, 15(1), pp.3741-3782.

3. Kalisch, M., Machler, M., Colombo, D., Maathuis, M.H. and Buhlmann, P., 2012. Causal inference using graphical models with the R package pcalg. *Journal of Statistical Software*, 47(11), pp.1-26.

4. Hauser, A. and Buhlmann, P., 2012. Characterization and greedy learning of interventional Markov equivalence classes of directed acyclic graphs. *Journal of Machine Learning Research*, 13(Aug), pp.2409-2464.

See Also

[getResiduals](#)

Examples

```
data(simdata)
out <- pcgen(simdata)

data(simdata)
rs <- getResiduals(suffStat = simdata)
pc.fit1 <- pcgen(suffStat = simdata, alpha = 0.01, verbose = TRUE,
                use.res = TRUE, res.cor = cor(rs))
```

pcgenFast

pcgen with residual-based screening

Description

The pcgen algorithm starting with a skeleton estimated using the standard pc-algorithm, based on residuals from the GBLUP.

Usage

```
pcgenFast(suffStat, alpha = 0.01, m.max = Inf, res.m.max = Inf, verbose = FALSE,
          covariates = NULL, fixedEdges = NULL, QTLs = integer(), max.iter = 50,
          stop.if.significant = TRUE, cov.method = 'uni', use.res = FALSE,
          return.pvalues = FALSE)
```

Arguments

suffStat	A data.frame, of which the first column is the factor G (genotype), and subsequent columns contain the traits, and optionally some QTLs. The name of the first column should be G.
alpha	The significance level used in each conditional independence test. Default is 0.01.

<code>m.max</code>	Maximum size of the conditioning set, in the pcgen algorithm.
<code>res.m.max</code>	Maximum size of the conditioning set, in the pc-algorithm on the residuals (used for prior screening).
<code>verbose</code>	If TRUE, p-values for the conditional independence tests are printed.
<code>covariates</code>	A data.frame containing covariates, to be used in each conditional independence test. Cannot contain factors. Should be either NULL (default) or a data.frame with the same number of rows as <code>suffStat</code> . An intercept is already included for each trait in <code>suffStat</code> ; covariates should not contain a column of ones.
<code>fixedEdges</code>	A logical matrix of dimension $(p + 1) \times (p + 1)$, where p is the number of traits. The first row and column refer to the node G, and subsequent rows and columns to the traits. As in the <code>pcalg</code> package, the edge $i - j$ is never considered for removal if the entry $[i, j]$ or $[j, i]$ (or both) are TRUE. In that case, the edge is guaranteed to be present in the resulting graph.
<code>QTLs</code>	Column numbers in <code>suffStat</code> that correspond to QTLs.
<code>max.iter</code>	Maximum number of iterations in the EM-algorithm, used to fit the bivariate mixed model (when <code>use.res = FALSE</code>).
<code>stop.if.significant</code>	If TRUE, the EM-algorithm used in some of the conditional independence tests (when <code>use.res = FALSE</code>) will be stopped whenever the p-value becomes significant, i.e. below <code>alpha</code> . This will speed up calculations, and can be done because (1) the PC algorithm only needs an accept/reject decision (2) In EM the likelihood is nondecreasing. Should be put to FALSE if the precise p-values are of interest.
<code>cov.method</code>	A string, specifying which method should be used to compute the GBLUP. Options are 'us' (unstructured multi-trait model fitted using sommer) and 'uni' (based on univariate GBLUPs). Default is 'uni'.
<code>use.res</code>	If FALSE, residuals from GBLUP are only used for screening with the standard pc algorithm. After that, the standard pcgen algorithm is run on the remaining edges; the test for conditional independence of 2 traits given a set of other traits and G is based on bivariate mixed models. If TRUE, this test is based on the residuals. In this case, no further edges between traits are removed after screening and pcgen will only infer the orientation, and the direct genetic effects.
<code>return.pvalues</code>	If TRUE, the maximal p-value for each edge is returned.

Value

If `return.pvalues = FALSE`, the output is a graph (an object with S3 class "pcgen"). If `return.pvalues = TRUE`, the output is a list with elements `gr` (the graph) and `pMax` (a matrix with the p-values).

Author(s)

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References

1. Kruijjer, W., Behrouzi, P., Rodriguez-Alvarez, M. X., Wit, E. C., Mahmoudi, S. M., Yandell, B., Van Eeuwijk, F., (2018, in preparation), Reconstruction of networks with direct and indirect genetic effects.
2. Colombo, D. and Maathuis, M.H., 2014. Order-independent constraint-based causal structure learning. *The Journal of Machine Learning Research*, 15(1), pp.3741-3782.

See Also

[getResiduals](#)

Examples

```
data(simdata)
out <- pcgenFast(suffStat = simdata, alpha = 0.01, verbose= FALSE, use.res = TRUE)
```

pcgenTest

The conditional independence test in pcgen

Description

This performs the conditional independence test used in the pcgen algorithm, assuming there are replicates, and independent genetic effects.

Usage

```
pcgenTest(x, y, S, suffStat, QTLs = integer(), covariates = NULL, alpha = 0.01,
          max.iter = 50, stop.if.significant = TRUE, use.res = FALSE, res.cor = NULL)
```

Arguments

<code>x, y</code>	Column numbers in <code>suffStat</code> that should be tested for conditional independence given the variables in <code>S</code> .
<code>S</code>	vector of integers defining the conditioning set, where the integers refer to column numbers in <code>suffStat</code> . May be <code>numeric()</code> , i.e. the empty set.
<code>suffStat</code>	A <code>data.frame</code> , of which the first column is the factor <code>G</code> (genotype), and subsequent columns contain the traits, and optionally some QTLs. The name of the first column should be <code>G</code> . It should not contain covariates.
<code>QTLs</code>	Column numbers in <code>suffStat</code> that correspond to QTLs. These may be partly in <code>S</code> and <code>x</code> and <code>y</code> , but <code>x</code> and <code>y</code> cannot be both QTLs.
<code>covariates</code>	A <code>data.frame</code> containing covariates. It should be either <code>NULL</code> (default) or a <code>data.frame</code> with the same number of rows as <code>suffStat</code> . An intercept is already included for each trait in <code>suffStat</code> ; covariates should not contain a column of ones.

<code>alpha</code>	The significance level used in the test. The test itself of course does not depend on this, but it is used in the EM-algorithm to speed up calculations. When <code>stop.if.significant = TRUE</code> , the EM-algorithm is stopped once the p-value is below the significance level. Default is 0.01.
<code>max.iter</code>	Maximum number of iterations in the EM-algorithm, used to fit the bivariate mixed model (when <code>use.res = FALSE</code>).
<code>stop.if.significant</code>	If TRUE, the EM-algorithm used in some of the conditional independence tests (when <code>use.res = FALSE</code>) will be stopped whenever the p-value becomes significant, i.e. below alpha. This will speed up calculations, and can be done because (1) the PC algorithm only needs an accept/reject decision (2) In EM the likelihood is nondecreasing. It should be put to FALSE if the precise p-value is of interest.
<code>use.res</code>	If TRUE, the test for conditional independence of 2 traits given a set of other traits and G is based on residuals from GBLUP. If FALSE (the default), it is based on bivariate mixed models.
<code>res.cor</code>	If <code>use.res = TRUE</code> , <code>res.cor</code> should be the correlation matrix of the residuals from the GBLUP. These can be obtained with the <code>getResiduals</code> function. See the example below.

Details

`pcgenTest` tests for conditional independence between x and y given S . It distinguishes 2 situations: (i) if one of x and y (say x) is the factor G, `pcgenTest` will test if the genetic variance in y is zero, given the traits in S . (ii) if x and y are both traits, `pcgenTest` tests if the residual covariance between them is zero, given the traits in S and the factor G. The factor G is automatically included in the conditioning set S (S does not need to contain the integer 1). This test is either based on a bivariate mixed model (when `use.res=FALSE`), or on residuals from GBLUP (`use.res=T`), obtained with the `getResiduals` function. In the latter case, `res.cor` must be provided.

Value

A p-value

Author(s)

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References

Kruijer, W., Behrouzi, P., Rodriguez-Alvarez, M. X., Wit, E. C., Mahmoudi, S. M., Yandell, B., Van Eeuwijk, F., (2018, in preparation), Reconstruction of networks with direct and indirect genetic effects.

See Also

[getResiduals](#)

Examples

```

data(simdata)
rs <- getResiduals(suffStat= simdata)
pcgenTest(suffStat= simdata, x= 2, y= 3, S= 4)
pcgenTest(suffStat= simdata, x= 2, y= 3, S= c(1,4))
pcgenTest(suffStat= simdata, x= 2, y= 3, S= 4, use.res= TRUE, res.cor= cor(rs))
pcgenTest(suffStat= simdata, x= 2, y= 1, S= 4)

```

pcRes

The pc algorithm applied to residuals

Description

The standard pc algorithm applied to GBLUP residuals, or to the GBLUP itself.

Usage

```

pcRes(suffStat, alpha= 0.01, K = NULL, m.max = Inf, verbose = FALSE,
      covariates = NULL, QTLs = integer(), cov.method = "uni",
      use.GBLUP = FALSE, return.pvalues = FALSE)

```

Arguments

suffStat	A data.frame, of which the first column is the factor G (genotype), and subsequent columns contain the traits, and optionally some QTLs. The name of the first column should be G.
alpha	The significance level used in the test. Default is 0.01.
K	A genetic relatedness matrix. If NULL (the default), independent genetic effects are assumed.
m.max	Maximum size of the conditioning set, in the pc-algorithm on the residuals.
verbose	If TRUE, p-values for the conditional independence tests are printed.
covariates	A data.frame containing covariates, that should always be used in each conditional independence test. Should be either NULL (default) or a data.frame with the same number of rows as suffStat. An intercept is already included for each trait in suffStat; covariates should not contain a column of ones.
QTLs	Column numbers in suffStat that correspond to QTLs.
cov.method	A string, specifying which method should be used to compute the GBLUP. Options are 'us' (unstructured multi-trait model fitted using sommer) and 'uni' (based on univariate GBLUPs).
use.GBLUP	Use the GBLUP itself, instead of the residuals
return.pvalues	If TRUE, the maximal p-value for each edge is returned.

Details

If `use.GBLUP = FALSE`, GBLUP residuals are used as input for the pc-stable algorithm of Colombo and Maathuis (2014). This closely resembles the residual networks of Valente et al., (2010) and Topner et al., (2017) (who used different ways to predict the genetic effects, and applied other causal inference algorithms to the residuals). When `use.GBLUP = TRUE`, pc-stable is applied to the GBLUP itself, which resembles the genomic networks of Topner et al., (2017). If `cov.method = "uni"`, the GBLUP and the residuals are computed separately for each trait in `suffStat`. The covariance of each trait is assumed to be

$$\sigma_G^2 Z K Z^t + \sigma_E^2 I_n$$

where Z is a binary incidence matrix, assigning plants or plots to genotypes. Z is based on the first column in `suffStat`. If there is a single observation per genotype (typically a genotypic mean), Z is the identity matrix, and the relatedness matrix K should be specified. If there are replicates for at least some of the genotypes, and no K is provided, independent genetic effects are assumed (K will be the identity matrix). It is also possible to have replicates and specify a non-diagonal K . Whenever K is specified, `sommer (mmer2)` will be used; otherwise `lmer (lme4)`. `mmer2` is also used when `cov.method = "us"`, in which case the multivariate GBLUP is computed, for all traits in `suffStat` simultaneously. This is only possible for a limited number of traits.

Value

If `return.pvalues = FALSE`, the output is a graph (an object with S3 class "pcgen"). If `return.pvalues = TRUE`, the output is a list with elements `gr` (the graph) and `pMax` (a matrix with the p-values).

Author(s)

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References

1. Colombo, D. and Maathuis, M.H., 2014. Order-independent constraint-based causal structure learning. *The Journal of Machine Learning Research*, 15(1), pp.3741-3782.
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3. Topner, K., Rosa, G.J., Gianola, D. and Schon, C.C., 2017. Bayesian Networks Illustrate Genomic and Residual Trait Connections in Maize (*Zea mays* L.). *G3: Genes, Genomes, Genetics*, pp.g3-117.
4. Valente, B.D., Rosa, G.J., Gustavo, A., Gianola, D. and Silva, M.A., 2010. Searching for recursive causal structures in multivariate quantitative genetics mixed models. *Genetics*.

Examples

```
data(simdata)
out <- pcRes(suffStat = simdata, alpha = 0.01, verbose= FALSE)
```

simdata	<i>Simulated data</i>
---------	-----------------------

Description

Simulated data, for two replicates of genotypes g_1, \dots, g_{200} . Three traits were simulated (Y1, Y2 and Y3), using a structural equation model defined by $Y_1 \rightarrow Y_2 \rightarrow Y_3$, and direct genetic effects on Y1 and Y3.

Usage

```
data(simdata)
```

Format

A data frame of dimension 4×400 . The first column is the factor G (genotype); the subsequent columns contain y_1, y_2 and y_3 .

Examples

```
data(simdata)
out <- pcgen(simdata)
out2 <- pcRes(suffStat = simdata, alpha = 0.01, verbose= FALSE)
```

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