

Package ‘mwTensor’

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Type Package

Title Multi-Way Component Analysis

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Suggests testthat

Depends R (>= 4.1.0)

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Description For single tensor data, any matrix factorization method can be specified the matrixed tensor in each dimension by Multi-way Component Analysis (MWCA). An originally extended MWCA is also implemented to specify and decompose multiple matrices and tensors simultaneously (CoupledMWCA). See the reference section of GitHub README.md <<https://github.com/rikenbit/mwTensor>>, for details of the methods.

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URL <https://github.com/rikenbit/mwTensor>

NeedsCompilation no

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mwTensor-package	<i>Multi-Way Component Analysis</i>
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Description

For single tensor data, any matrix factorization method can be specified the matricised tensor in each dimension by Multi-way Component Analysis (MWCA). An originally extended MWCA is also implemented to specify and decompose multiple matrices and tensors simultaneously (CoupledMWCA). See the reference section of GitHub README.md <<https://github.com/rikenbit/mwTensor>>, for details of the methods.

Details

The DESCRIPTION file:

```

Package:      mwTensor
Type:         Package
Title:        Multi-Way Component Analysis
Version:      0.99.6
Date:         2022-6-15
Authors@R:   c(person("Koki", "Tsuyuzaki", role = c("aut", "cre"), email = "k.t.the-answer@hotmail.co.jp"))
Suggests:    testthat
Depends:      R (>= 4.1.0)
Imports:      methods, MASS, rTensor, nnTensor, ccTensor, iTensor, igraph
Description:  For single tensor data, any matrix factorization method can be specified the matricised tensor in each dimension
License:      Artistic-2.0
URL:          https://github.com/rikenbit/mwTensor
Author:       Koki Tsuyuzaki [aut, cre]
Maintainer:   Koki Tsuyuzaki <k.t.the-answer@hotmail.co.jp>

```

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CoupledMWCAResult-class  Class "CoupledMWCAResult"

```

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MWCAResult-class	Class "MWCAResult"
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myCX	CX Decomposition as an example of user-defined matrix decomposition.
myICA	Independent Component Analysis (ICA) as an example of user-defined matrix decomposition.
myNMF	Independent Component Analysis (ICA) as an example of user-defined matrix decomposition.
mySVD	Singular Value Decomposition (SVD) as an example of user-defined matrix decomposition.
plotTensor3Ds	Plot function for visualization of tensor data structure
toyModel	Toy model of coupled tensor data

Author(s)

NA

Maintainer: NA

References

- Andrzej Cichocki et al., (2016). Tensor Networks for Dimensionality Reduction and Large-scale Optimization: Part 1 Low-Rank Tensor Decompositions
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- Andrzej CICHOCKI, et. al., (2009). Nonnegative Matrix and Tensor Factorizations.
- A. Hyvarinen. (1999). Fast and Robust Fixed-Point Algorithms for Independent Component Analysis. *IEEE Transactions on Neural Networks*, 10(3), 626-634.
- Petros Drineas et al., (2008). Relative-Error CUR Matrix Decompositions, *SIAM Journal on Matrix Analysis and Applications*, 30(2), 844-881.

See Also

[mySVD](#), [myALS_SVD](#), [myNMF](#), [myICA](#), [myCX](#), [MWCA](#), [CoupledMWCA](#), [plotTensor3Ds](#)

Examples

```
ls("package:mwTensor")
```

CoupledMWCA

Coupled Multi-way Component Analysis (CoupledMWCA)

Description

The input is assumed to be a CoupledMWCAParams object.

Usage

```
CoupledMWCA(params)
```

Arguments

params CoupledMWCAParams object

Value

CoupledMWCAResult object.

Author(s)

Koki Tsuyuzaki

See Also

[CoupledMWCAParams-class](#) and [CoupledMWCAResult-class](#).

Examples

```
if(interactive()){  
# Test data (multiple arrays)  
  Xs <- toyModel("coupled_CP_Easy")  
  
  params <- new("CoupledMWCAParams", Xs=Xs)  
  out <- CoupledMWCA(params)  
}
```

 CoupledMWCAParams-class

Class "CoupledMWCAParams"

Description

The parameter object to be specified against CoupledMWCA function.

Objects from the Class

Objects can be created by calls of the form `new("CoupledMWCAParams", ...)`.

Slots

MWCAParams has four settings as follows. For each setting, the list must have the same structure.

1. Data-wise setting Each item must be a list object that is as long as the number of data and is named after the data.

A list containing multiple high-dimensional arrays.

mask: A list containing multiple high-dimensional arrays, in which 0 or 1 values are filled to specify the missing elements.

weights: A list containing multiple high-dimensional arrays, in which some numeric values are specified to weigh each data.

2. Common Model setting Each item must be a nested list object that is as long as the number of data and is named after the data.

common_model: Each element of the list must be a list corresponding the dimension name of data and common factor matrices name.

3. Common Factor matrix-wise setting Each item must be a list object that is as long as the number of common factor matrices and is named after the factor matrices.

common_initial: The initial values of common factor matrices. If nothing is specified, random matrices are used.

common_algorithms: Algorithms used to decompose the matricised tensor in each mode.

common_iteration: The number of iterations.

common_decomp: If FALSE is specified, unit matrix is used as the common factor matrix.

common_fix: If TRUE is specified, the common factor matrix is not updated in the iteration.

common_dims: The lower dimension of each common factor matrix.

common_transpose: Whether the common factor matrix is transposed to calculate core tensor.

common_coretype: If "CP" is specified, all the core tensors become diagonal core tensors. If "Tucker" is specified, all the core tensors become dense core tensors.

4. Specific Model setting Each item must be a nested list object that is as long as the number of data and is named after the data.

specific_model: Each element of the list must be a list corresponding the dimension name of data and data specific factor matrices name.

5. *Specific Factor matrix-wise setting* Each item must be a list object that is as long as the number of data specific factor matrices and is named after the factor matrices.

specific_initial: The initial values of data specific factor matrices. If nothing is specified, random matrices are used.

specific_algorithms: Algorithms used to decompose the matricised tensor in each mode.

specific_iteration: The number of iterations.

specific_decomp: If FALSE is specified, unit matrix is used as the data specific factor matrix.

specific_fix: If TRUE is specified, the data specific factor matrix is not updated in the iteration.

specific_dims: The lower dimension of each data specific factor matrix.

specific_transpose: Whether the data specific factor matrix is transposed to calculate core tensor.

specific_coretype: If "CP" is specified, all the core tensors become diagonal core tensors. If "Tucker" is specified, all the core tensors become dense core tensors.

6. *Other option* Each item must to be a vector of length 1.

specific: Whether data specific factor matrices are also calculated.

thr: The threshold to stop the iteration. The higher the value, the faster the iteration will stop.

viz: Whether the output is visualized.

figdir: When viz=TRUE, whether the plot is output in the directory.

verbose: Whether the process is monitored by verbose messages.

Methods

CoupledMWCA Function to perform CoupledMWCA.

See Also

[CoupledMWCAResult-class](#), [CoupledMWCA](#)

CoupledMWCAResult-class

Class "CoupledMWCAResult"

Description

The result object generated by CoupledMWCA function.

Slots

weights: weights of CoupledMWCAParams.
common_model: common_model of CoupledMWCAParams.
common_initial: common_initial of CoupledMWCAParams.
common_algorithms: common_algorithms of CoupledMWCAParams.
common_iteration: common_iteration of CoupledMWCAParams.
common_decomp: common_decomp of CoupledMWCAParams.
common_fix: common_fix of CoupledMWCAParams.
common_dims: common_dims of CoupledMWCAParams.
common_transpose: common_transpose of CoupledMWCAParams.
common_coretype: common_coretype of CoupledMWCAParams.
common_factors: Common factor matrices of CoupledMWCA.
common_cores: Common core tensors of CoupledMWCA.
specific_model: specific_model of CoupledMWCAParams.
specific_initial: specific_initial of CoupledMWCAParams.
specific_algorithms: specific_algorithms of CoupledMWCAParams.
specific_iteration: specific_iteration of CoupledMWCAParams.
specific_decomp: specific_decomp of CoupledMWCAParams.
specific_fix: specific_fix of CoupledMWCAParams.
specific_dims: specific_dims of CoupledMWCAParams.
specific_transpose: specific_transpose of CoupledMWCAParams.
specific_coretype: specific_coretype of CoupledMWCAParams.
specific_factors: Data specific factor matrices of CoupledMWCA.
specific_cores: Data specific core tensors of CoupledMWCA.
specific: specific of CoupledMWCAParams.
thr: thr of CoupledMWCAParams.
viz: viz of CoupledMWCAParams.
figdir: figdir of CoupledMWCAParams.
verbose: verbose of CoupledMWCAParams.
rec_error: The reconstructed error.
train_error: Training Error. $\text{train_error} + \text{test_error} = \text{rec_error}$.
test_error: Test Error. $\text{train_error} + \text{test_error} = \text{rec_error}$.
rel_change: The relative change of each iteration step.

See Also

[CoupledMWCAParams-class](#), [CoupledMWCA](#)

MWCA

Multi-way Component Analysis (MWCA)

Description

The input is assumed to be a `MWCAParams` object.

Usage

```
MWCA(params)
```

Arguments

`params` `MWCAParams` object

Value

`MWCAResult` object.

Author(s)

Koki Tsuyuzaki

References

Andrzej Cichocki et al., (2016). Tensor Networks for Dimensionality Reduction and Large-scale Optimization: Part 1 Low-Rank Tensor Decompositions

Andrzej Cichocki et al., (2015). Tensor Decompositions for Signal Processing Applications, *IEEE SIGNAL PROCESSING MAGAZINE*

See Also

[MWCAParams-class](#) and [MWCAResult-class](#).

Examples

```
if(interactive()){  
  # Test data (single array)  
  X <- nnTensor::toyModel("Tucker")@data  
  
  params <- new("MWCAParams", X=X)  
  out <- MWCA(params)  
}
```

MWCAParams-class	Class "MWCAParams"
------------------	--------------------

Description

The parameter object to be specified against MWCA function.

Objects from the Class

Objects can be created by calls of the form `new("MWCAParams", ...)`.

Slots

X: A high-dimensional array.

mask: A mask array having the same dimension of X.

algorithms: Algorithms used to decompose the matricised tensor in each mode.

dims: The lower dimension of each factor matrix.

transpose: Whether the factor matrix is transposed to calculate core tensor.

viz: Whether the output is visualized.

figdir: When viz=TRUE, whether the plot is output in the directory.

Methods

MWCA Function to perform MWCA.

See Also

[MWCAResult-class](#), [MWCA](#)

MWCAResult-class	Class "MWCAResult"
------------------	--------------------

Description

The result object generated by MWCA function.

Slots

algorithms: algorithm of MWCAParams.

dims: dims of MWCAParams.

transpose: transpose of MWCAParams.

viz: viz of MWCAParams.

figdir: figdir of MWCAParams.

factors: The factor matrices of MWCA.

core: The core tensor of MWCA.

rec_error: The reconstructed error.

train_error: Training Error. $\text{train_error} + \text{test_error} = \text{rec_error}$.

test_error: Test Error. $\text{train_error} + \text{test_error} = \text{rec_error}$.

See Also

[MWCAParams-class](#), [MWCA](#)

myALS_SVD

*Alternating Least Square Singular Value Decomposition (ALS-SVD)
as an example of user-defined matrix decomposition.*

Description

The input data is assumed to be a matrix. When algorithms of MWCAParams and CoupledMWCA-Params are specified as "myALS_SVD", This function is called in MWCA and CoupledMWCA.

Usage

```
myALS_SVD(Xn, k, L2=1e-10, iter=30)
```

Arguments

Xn	The input matrix which has N-rows and M-columns.
k	The rank parameter ($k \leq \min(N,M)$)
L2	The regularization parameter (Default: 1e-10)
iter	The number of iteration (Default: 30)

Value

The output matrix which has N-rows and k-columns.

Author(s)

Koki Tsuyuzaki

References

Madeleine Udell et al., (2016). Generalized Low Rank Models, *Foundations and Trends in Machine Learning*, 9(1).

Examples

```
if(interactive()){
  # Test data
  matdata <- matrix(runif(10*20), nrow=10, ncol=20)
  myALS_SVD(matdata, k=3, L2=0.1, iter=10)
}
```

myCX	<i>CX Decomposition as an example of user-defined matrix decomposition.</i>
------	---

Description

The input data is assumed to be a matrix. When algorithms of MWCAParams and CoupledMWCAParams are specified as "myCX", This function is called in MWCA and CoupledMWCA.

Usage

```
myCX(Xn, k)
```

Arguments

Xn	The input matrix which has N-rows and M-columns.
k	The rank parameter ($k \leq \min(N,M)$)

Value

The output matrix which has N-rows and k-columns.

Author(s)

Koki Tsuyuzaki

References

Petros Drineas et al., (2008). Relative-Error CUR Matrix Decompositions, *SIAM Journal on Matrix Analysis and Applications*, 30(2), 844-881.

Examples

```
if(interactive()){
  # Test data
  matdata <- matrix(runif(10*20), nrow=10, ncol=20)
  myCX(matdata, k=3)
}
```

myICA	<i>Independent Component Analysis (ICA) as an example of user-defined matrix decomposition.</i>
-------	---

Description

The input data is assumed to be a matrix. When algorithms of MWCAParams and CoupledMWCAParams are specified as "myICA", This function is called in MWCA and CoupledMWCA.

Usage

```
myICA(Xn, k)
```

Arguments

Xn	The input matrix which has N-rows and M-columns.
k	The rank parameter ($k \leq \min(N,M)$)

Value

The output matrix which has N-rows and k-columns.

Author(s)

Koki Tsuyuzaki

References

A. Hyvarinen. (1999). Fast and Robust Fixed-Point Algorithms for Independent Component Analysis. *IEEE Transactions on Neural Networks*, 10(3), 626-634.

Examples

```
if(interactive()){  
  # Test data  
  matdata <- matrix(runif(10*20), nrow=10, ncol=20)  
  myICA(matdata, k=3)  
}
```

myNMF	<i>Independent Component Analysis (ICA) as an example of user-defined matrix decomposition.</i>
-------	---

Description

The input data is assumed to be a matrix. When algorithms of MWCAParams and CoupledMWCAParams are specified as "myNMF", This function is called in MWCA and CoupledMWCA.

Usage

```
myNMF(Xn, k, L1=1e-10, L2=1e-10)
```

Arguments

Xn	The input matrix which has N-rows and M-columns.
k	The rank parameter ($k \leq \min(N,M)$)
L1	The regularization parameter to control the sparseness (Default: 1e-10)
L2	The regularization parameter to control the overfit (Default: 1e-10)

Value

The output matrix which has N-rows and k-columns.

Author(s)

Koki Tsuyuzaki

References

Andrzej CICHOCK, et. al., (2009). Nonnegative Matrix and Tensor Factorizations.

Examples

```
if(interactive()){  
  # Test data  
  matdata <- matrix(runif(10*20), nrow=10, ncol=20)  
  myNMF(matdata, k=3, L1=1e-1, L2=1e-2)  
}
```

mySVD	<i>Singular Value Decomposition (SVD) as an example of user-defined matrix decomposition.</i>
-------	---

Description

The input data is assumed to be a matrix. When algorithms of MWCAParams and CoupledMWCAParams are specified as "mySVD", This function is called in MWCA and CoupledMWCA.

Usage

```
mySVD(Xn, k)
```

Arguments

Xn	The input matrix which has N-rows and M-columns.
k	The rank parameter ($k \leq \min(N,M)$)

Value

The output matrix which has N-rows and k-columns.

Author(s)

Koki Tsuyuzaki

Examples

```
if(interactive()){  
  # Test data  
  matdata <- matrix(runif(10*20), nrow=10, ncol=20)  
  mySVD(matdata, k=3)  
}
```

plotTensor3Ds	<i>Plot function for visualization of tensor data structure</i>
---------------	---

Description

Multiple multi-dimensional arrays and matrices are visualized simultaneously.

Usage

```
plotTensor3Ds(Xs)
```

Arguments

`Xs` A List object containing multi-dimensional array (or matrix) in each element.

Author(s)

Koki Tsuyuzaki

See Also

[plotTensor3D](#) and [plotTensor2D](#).

Examples

```
Xs <- toyModel(model = "coupled_CP_Easy")

tmp <- tempdir()

png(filename=paste0(tmp, "/couled_CP.png"))
plotTensor3Ds(Xs)
dev.off()
```

toyModel

Toy model of coupled tensor data

Description

A list object containing multiple arrays are generated.

Usage

```
toyModel(model = "coupled_CP_Easy", seeds=123)
```

Arguments

`model` "coupled_CP_Easy", "coupled_CP_Hard", "coupled_Tucker_Easy", "coupled_Tucker_Hard", "coupled_Complex_Easy", or "coupled_Complex_Hard" can be specified (Default: "coupled_CP_Easy").

`seeds` The seed of random number (Default: 123).

Author(s)

Koki Tsuyuzaki

Examples

```
Xs <- toyModel(model = "coupled_CP_Easy", seeds=123)
```

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