

Package ‘growthmodels’

February 20, 2015

Type Package

Title Nonlinear Growth Models

Version 1.2.0

Date 2013-11-23

Author Daniel Rodriguez Perez

Maintainer Daniel Rodriguez Perez <daniel.rodriguez.perez@gmail.com>

Description A compilation of nonlinear growth models used in many areas

License GPL-3

URL <https://github.com/drodriguezperez/growthmodels>

BugReports <https://github.com/drodriguezperez/growthmodels/issues>

Collate 'negativeExponential.R' 'monomolecular.R' 'mitcherlich.R'
'gompertz.R' 'logistic.R' 'chapmanRichards.R' 'richard.R'
'vonBertalanffy.R' 'weibull.R' 'loglogistic.R' 'mmf.R'
'schnute.R' 'stannard.R' 'brody.R' 'growthmodels.R'
'blumberg.R'

NeedsCompilation no

Repository CRAN

Date/Publication 2013-11-23 17:11:06

R topics documented:

growthmodels-package	2
blumberg	3
brody	4
chapmanRichards	4
generalisedLogistic	5
generalisedRichard	6
gompertz	7
logistic	8
loglogistic	8
mitcherlich	9

mmf	10
monomolecular	11
negativeExponential	11
richard	12
schnute	13
stannard	14
vonBertalanffy	14
weibull	15

Index	17
--------------	-----------

growthmodels-package *growthmodels: Nonlinear Growth Models*

Description

A compilation of nonlinear growth models used in many areas.

Details

Package: growthmodels
Version: 1.2.0
License: GPL-3

Author(s)

Daniel Rodriguez Perez <daniel.rodriguez.perez@gmail.com>

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

M. M. Kaps, W. O. W. Herring, and W. R. W. Lamberson, "Genetic and environmental parameters for traits derived from the Brody growth curve and their relationships with weaning weight in Angus cattle.," *Journal of Animal Science*, vol. 78, no. 6, pp. 1436-1442, May 2000.

A. Tsoularis and J. Wallace, "Analysis of logistic growth models.," *Math Biosci*, vol. 179, no. 1, pp. 21-55, Jul. 2002.

A. Khamiz, Z. Ismail, and A. T. Muhammad, "Nonlinear growth models for modeling oil palm yield growth," *Journal of Mathematics and Statistics*, vol. 1, no. 3, p. 225, 2005.

http://en.wikipedia.org/wiki/Generalised_logistic_function

blumberg	<i>Blumberg growth model</i>
----------	------------------------------

Description

Computes the Blumberg growth model and its inverse

$$y(t) = \frac{\alpha * (t + t_0)^m}{w_0 + (t + t_0)^m}$$

Usage

```
blumberg(t, alpha, w0, m, t0 = 0)
```

```
blumberg.inverse(x, alpha, w0, m, t0 = 0)
```

Arguments

t	time
x	size
alpha	upper asymptote
w0	a reference value at t = t0
m	slope of growth
t0	time shift (default 0)

References

A. Tsoularis and J. Wallace, "Analysis of logistic growth models.," Math Biosci, vol. 179, no. 1, pp. 21-55, Jul. 2002.

Examples

```
growth <- blumberg(0:10, 10, 2, 0.5)
# Calculate inverse function
time <- blumberg.inverse(growth, 12, 2, 0.5)
```

 brody

Brody growth model

Description

Computes the Brody growth model and its inverse

$$y(t) = \alpha - (\alpha - w_0)\exp(-kt)$$

Usage

```
brody(t, alpha, w0, k)
```

```
brody.inverse(x, alpha, w0, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
w0	the value at t = 0
k	growth rate

References

M. M. Kaps, W. O. W. Herring, and W. R. W. Lamberson, "Genetic and environmental parameters for traits derived from the Brody growth curve and their relationships with weaning weight in Angus cattle.," *Journal of Animal Science*, vol. 78, no. 6, pp. 1436-1442, May 2000.

Examples

```
growth <- brody(0:10, 10, 5, 0.3)
# Calculate inverse function
time <- brody.inverse(growth, 10, 5, 0.3)
```

 chapmanRichards

Chapman-Richards growth model

Description

Computes the Chapman-Richards growth model and its inverse

$$y(t) = \alpha(1 - \beta\exp(-kt))^{1/(1-m)}$$

Usage

```
chapmanRichards(t, alpha, beta, k, m)

chapmanRichards.inverse(x, alpha, beta, k, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate
m	slope of growth

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- chapmanRichards(0:10, 10, 0.5, 0.3, 0.5)
# Calculate inverse function
time <- chapmanRichards.inverse(growth, 10, 0.5, 0.3, 0.5)
```

generalisedLogistic *Generalised Logistic growth model*

Description

Computes the Generalised Logistic growth model

$$y(t) = A + \frac{U - A}{1 + \beta \exp(-k(t - t_0))}$$

Usage

```
generalisedLogistic(t, A, U, k, beta, t0)

generalisedLogistic.inverse(x, A, U, k, beta, t0 = 0)
```

Arguments

t	time
x	size
A	the lower asymptote
U	the upper asymptote
k	growth range
beta	growth range
t0	time shift (default 0)

References

http://en.wikipedia.org/wiki/Generalised_logistic_function

Examples

```
growth <- generalisedLogistic(0:10, 5, 10, 0.3, 0.5, 3)
# Calculate inverse function
time <- generalisedLogistic.inverse(growth, 5, 10, 0.3, 0.5, 3)
```

generalisedRichard *Generalised Richard growth model*

Description

Computes the Generalised Richard growth model and its inverse

$$y(t) = A + \frac{U - A}{(1 + \beta \exp(-k(t - t_0)))^{(1/m)}}$$

Usage

```
generalisedRichard(t, A, U, k, m, beta, t0)
```

```
generalisedRichard.inverse(x, A, U, k, m, beta, t0 = 0)
```

Arguments

t	time
x	size
A	the lower asymptote
U	the upper asymptote
k	growth range
m	slope of growth
beta	growth range
t0	time shift (default 0)

References

http://en.wikipedia.org/wiki/Generalised_logistic_function

Examples

```
growth <- generalisedRichard(0:10, 5, 10, 0.3, 0.5, 1, 3)
time <- generalisedRichard.inverse(growth, 5, 10, 0.3, 0.5, 1, 3)
```

gompertz

Gompertz growth model

Description

Computes the Gompertz growth model and its inverse

$$y(t) = \alpha \exp(-\beta \exp(-k^t))$$

Usage

```
gompertz(t, alpha, beta, k)

gompertz.inverse(x, alpha, beta, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth displacement
k	growth rate

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- gompertz(0:10, 10, 0.5, 0.3)
# Calculate inverse function
time <- gompertz.inverse(growth, 10, 0.5, 0.3)
```

 logistic

Logistic growth model

Description

Computes the Logistic growth model

$$y(t) = \frac{\alpha}{1 + \beta \exp(-kt)}$$

Usage

```
logistic(t, alpha, beta, k)
```

```
logistic.inverse(x, alpha, beta, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- logistic(0:10, 10, 0.5, 0.3)
# Calculate inverse function
time <- logistic.inverse(growth, 10, 0.5, 0.3)
```

 loglogistic

Log-logistic growth model

Description

Computes the Log-logistic growth model

$$y(t) = \frac{\alpha}{1 + \beta \exp(-k \log(t))}$$

Usage

```
loglogistic(t, alpha, beta, k)

loglogistic.inverse(x, alpha, beta, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate

References

A. Khamiz, Z. Ismail, and A. T. Muhammad, "Nonlinear growth models for modeling oil palm yield growth," *Journal of Mathematics and Statistics*, vol. 1, no. 3, p. 225, 2005.

Examples

```
growth <- loglogistic(0:10, 10, 0.5, 0.3)
# Calculate inverse function
time <- loglogistic.inverse(growth, 10, 0.5, 0.3)
```

mitcherlich

Mitcherlich growth model

Description

Computes the Mitcherlich growth model

$$y(t) = (\alpha - \beta k^t)$$

Usage

```
mitcherlich(t, alpha, beta, k)

mitcherlich.inverse(x, alpha, beta, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- mitcherlich(0:10, 10, 0.5, 0.3)
# Calculate inverse function
time <- mitcherlich.inverse(growth, 10, 0.5, 0.3)
```

mmf

*Morgan-Mercer-Flodin growth model***Description**

Computes the Morgan-Mercer-Flodin growth model

$$y(t) = \frac{(w_0\gamma + \alpha t^m)}{\gamma} + t^m$$

Usage

```
mmf(t, alpha, w0, gamma, m)

mmf.inverse(x, alpha, w0, gamma, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
w0	the value at t = 0
gamma	parameter that controls the point of inflection
m	growth rate

References

A. Khamiz, Z. Ismail, and A. T. Muhammad, "Nonlinear growth models for modeling oil palm yield growth," *Journal of Mathematics and Statistics*, vol. 1, no. 3, p. 225, 2005.

Examples

```
growth <- mmf(0:10, 10, 0.5, 4, 1)
# Calculate inverse function
time <- mmf.inverse(growth, 10, 0.5, 4, 1)
```

monomolecular	<i>Monomolecular growth model</i>
---------------	-----------------------------------

Description

Computes the monomolecular growth model

$$y(t) = \alpha(1 - \beta \exp(-kt))$$

Usage

```
monomolecular(t, alpha, beta, k)
```

```
monomolecular.inverse(x, alpha, beta, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- monomolecular(0:10, 10, 0.5, 0.3)
# Calculate inverse function
time <- monomolecular.inverse(growth, 10, 0.5, 0.3)
```

negativeExponential	<i>Negative exponential growth model</i>
---------------------	--

Description

Computes the negative exponential growth model

$$y(t) = \alpha(1 - \exp(-kt))$$

Usage

```
negativeExponential(t, alpha, k)

negativeExponential.inverse(x, alpha, k)
```

Arguments

t	time
x	size
alpha	upper asymptote
k	growth rate

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- negativeExponential(0:10, 1, 0.3)
# Calculate inverse function
time <- negativeExponential.inverse(growth, 10, 0.3)
```

 richard

Richard growth model

Description

Computes the Richard growth model and its inverse

$$y(t) = \frac{\alpha}{(1 + \beta \exp(-kt))^{(1/m)}}$$

Usage

```
richard(t, alpha, beta, k, m)

richard.inverse(x, alpha, beta, k, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate
m	slope of growth

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- richard(0:10, 10, 0.5, 0.3, 0.5)
time <- richard.inverse(growth, 10, 0.5, 0.3, 0.5)
```

schnute	<i>Schnute growth model</i>
---------	-----------------------------

Description

Computes the Schnute growth model

$$y(t) = [r_0 + \beta \exp(kt)]^m$$

Usage

```
schnute(t, r0, beta, k, m)

schnute.inverse(x, r0, beta, k, m)
```

Arguments

t	time
x	size
r0	reference value
beta	growth displacement
k	growth rate
m	slope of growth

References

A. Khamiz, Z. Ismail, and A. T. Muhammad, "Nonlinear growth models for modeling oil palm yield growth," *Journal of Mathematics and Statistics*, vol. 1, no. 3, p. 225, 2005.

Examples

```
growth <- schnute(0:10, 10, 5, .5, .5)
# Calculate inverse function
time <- schnute.inverse(growth, 10, 5, .5, .5)
```

stannard	<i>Stannard growth model</i>
----------	------------------------------

Description

Computes the Stannard growth model

$$y(t) = \alpha [1 + \exp(-(\beta + kt)/m)]^{-m}$$

Usage

```
stannard(t, alpha, beta, k, m)
```

```
stannard.inverse(x, alpha, beta, k, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth displacement
k	growth rate
m	slope of growth

References

A. Khamiz, Z. Ismail, and A. T. Muhammad, "Nonlinear growth models for modeling oil palm yield growth," *Journal of Mathematics and Statistics*, vol. 1, no. 3, p. 225, 2005.

Examples

```
growth <- stannard(0:10, 1, .2, .1, .5)
# Calculate inverse function
time <- stannard.inverse(growth, 1, .2, .1, .5)
```

vonBertalanffy	<i>von Bertalanffy growth model</i>
----------------	-------------------------------------

Description

Computes the von Bertalanffy growth model

$$y(t) = (\alpha^{1-m} - \beta * \exp(-kt))^{1/(1-m)}$$

Usage

```
vonBertalanffy(t, alpha, beta, k, m)
```

```
vonBertalanffy.inverse(x, alpha, beta, k, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate
m	slope of growth

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- vonBertalanffy(0:10, 10, 0.5, 0.3, 0.5)
# Calculate inverse function
time <- vonBertalanffy.inverse(growth, 10, 0.5, 0.3, 0.5)
```

weibull	<i>Weibull growth model</i>
---------	-----------------------------

Description

Computes the Weibull growth model

$$y(t) = \alpha - \beta \exp(-k * t^m)$$

Usage

```
weibull(t, alpha, beta, k, m)
```

```
weibull.inverse(x, alpha, beta, k, m)
```

Arguments

t	time
x	size
alpha	upper asymptote
beta	growth range
k	growth rate
m	slope of growth

References

D. Fekedulegn, M. Mac Siurtain, and J. Colbert, "Parameter estimation of nonlinear growth models in forestry," *Silva Fennica*, vol. 33, no. 4, pp. 327-336, 1999.

Examples

```
growth <- weibull(0:10, 10, 0.5, 0.3, 0.5)
# Calculate inverse function
time <- weibull.inverse(growth, 10, 0.5, 0.3, 0.5)
```


Index

blumberg, [3](#)

brody, [4](#)

chapmanRichards, [4](#)

generalisedLogistic, [5](#)

generalisedRichard, [6](#)

gompertz, [7](#)

growthmodels (growthmodels-package), [2](#)

growthmodels-package, [2](#)

logistic, [8](#)

loglogistic, [8](#)

mitcherlich, [9](#)

mmf, [10](#)

monomolecular, [11](#)

negativeExponential, [11](#)

richard, [12](#)

schmute, [13](#)

stannard, [14](#)

vonBertalanffy, [14](#)

weibull, [15](#)