

# Package ‘Copula.surv’

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**Type** Package

**Title** Analysis of Bivariate Survival Data Based on Copulas

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**Description** Simulating bivariate survival data from copula models.

Estimation of the association parameter in copula models.

Two different ways to estimate the association parameter in copula models are implemented.

A goodness-of-fit test for a given copula model is implemented.

See Emura, Lin and Wang (2010) <[doi:10.1016/j.csda.2010.03.013](https://doi.org/10.1016/j.csda.2010.03.013)> for details.

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Copula.surv-package     *Analysis of Bivariate Survival Data*

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### Description

Simulating bivariate survival data from copula models. Estimation of the association parameter in copula models. Two different ways to estimate the association parameter in copula models are implemented. A goodness-of-fit test for a given copula model is implemented. See Emura, Lin and Wang (2010) <doi:10.1016/j.csda.2010.03.013> for details.

### Details

Details are seen from the references.

### Author(s)

Takeshi Emura Maintainer: Takeshi Emura <takeshiemura@gmail.com>

### References

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

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simu.BB1     *Simulating data from the BB1 copula*

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### Description

$n$  pairs of  $(U,V)$  are generated from the BB1 copula.  $n$  pairs of  $(X,Y)$  are generated from the corresponding bivariate survival model with the Weibull marginal distributions. The default parameters (scale1=scale2=shape1=shape2=1) give the unit exponential distributions.

### Usage

```
simu.BB1(n, alpha, d=0, scale1=1, scale2=1, shape1=1, shape2=1)
```

### Arguments

n	sample size
alpha	association (copula) parameter
d	BB1 copula's departure parameter from the Clayton (d=0 is the default)
scale1	scale parameter for X
scale2	scale parameter for Y
shape1	shape parameter for X
shape2	shape parameter for Y

**Details**

See Section 2.6 of Emura et al.(2019) for copulas and bivariate survival times.

**Value**

U	uniformly distributed on (0,1)
V	uniformly distributed on (0,1)
X	Weibull distributed (scale1, shape1)
Y	Weibull distributed (scale2, shape2)

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Emura T, Matsui S, Rondeau V (2019), *Survival Analysis with Correlated Endpoints, Joint Frailty-Copula Models*, JSS Research Series in Statistics, Springer

**Examples**

```
n=100
Dat=simu.BB1(n=n, alpha=1, d=2, scale1=1, scale2=2, shape1=0.5, shape2=2)
plot(Dat[, "U"], Dat[, "V"])
cor(Dat[, "U"], Dat[, "V"], method="kendall")
plot(Dat[, "X"], Dat[, "Y"])
cor(Dat[, "X"], Dat[, "Y"], method="kendall")
```

---

simu.Clayton

*Simulating data from the Clayton copula*

---

**Description**

n pairs of (U,V) are generated from the Clayton copula. n paris of (X,Y) are generated from the corresponding bivariate survival model with the Weibull marginal distributions. The default parameters (scale1=scale2=shape1=shape2=1) give the unit exponential distributions.

**Usage**

```
simu.Clayton(n, alpha, scale1=1, scale2=1, shape1=1, shape2=1)
```

**Arguments**

n	sample size
alpha	association (copula) parameter
scale1	scale parameter for X
scale2	scale parameter for Y
shape1	shape parameter for X
shape2	shape parameter for Y

**Details**

See Section 2.6 of Emura et al.(2019) for copulas and bivariate survival times.

**Value**

U	uniformly distributed on (0,1)
V	uniformly distributed on (0,1)
X	Weibull distributed (scale1, shape1)
Y	Weibull distributed (scale2, shape2)

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Emura T, Matsui S, Rondeau V (2019), *Survival Analysis with Correlated Endpoints, Joint Frailty-Copula Models*, JSS Research Series in Statistics, Springer

**Examples**

```
n=100
Dat=simu.Clayton(n=n,alpha=1,scale1=1,scale2=2,shape1=0.5,shape2=2)
plot(Dat[,"U"],Dat[,"V"])
cor(Dat[,"U"],Dat[,"V"],method="kendall")
plot(Dat[,"X"],Dat[,"Y"])
cor(Dat[,"X"],Dat[,"Y"],method="kendall")
```

simu.FGM

*Simulating data from the FGM copula***Description**

$n$  pairs of  $(U, V)$  are generated from the FGM copula.  $n$  pairs of  $(X, Y)$  are generated from the corresponding bivariate survival model with the Weibull marginal distributions. The default parameters ( $\text{scale1}=\text{scale2}=\text{shape1}=\text{shape2}=1$ ) give the unit exponential distributions.

**Usage**

```
simu.FGM(n, alpha, scale1=1, scale2=1, shape1=1, shape2=1)
```

**Arguments**

<code>n</code>	sample size
<code>alpha</code>	association (copula) parameter; $-1 \leq \alpha \leq 1$
<code>scale1</code>	scale parameter for $X$
<code>scale2</code>	scale parameter for $Y$
<code>shape1</code>	shape parameter for $X$
<code>shape2</code>	shape parameter for $Y$

**Details**

See Section 2.6 of Emura et al.(2019) for copulas and bivariate survival times.

**Value**

<code>U</code>	uniformly distributed on $(0,1)$
<code>V</code>	uniformly distributed on $(0,1)$
<code>X</code>	Weibull distributed ( $\text{scale1}$ , $\text{shape1}$ )
<code>Y</code>	Weibull distributed ( $\text{scale2}$ , $\text{shape2}$ )

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Emura T, Matsui S, Rondeau V (2019), *Survival Analysis with Correlated Endpoints, Joint Frailty-Copula Models*, JSS Research Series in Statistics, Springer

**Examples**

```
n=100
Dat=simu.FGM(n=n,alpha=1,scale1=1,scale2=2,shape1=0.5,shape2=2)
plot(Dat[, "U"],Dat[, "V"])
cor(Dat[, "U"],Dat[, "V"],method="kendall")
plot(Dat[, "X"],Dat[, "Y"])
cor(Dat[, "X"],Dat[, "Y"],method="kendall")
```

---

simu.Frank

*Simulating data from the Frank copula*


---

**Description**

n pairs of (U,V) are generated from the Frank copula. n pairs of (X,Y) are generated from the corresponding bivariate survival model with the Weibull marginal distributions. The default parameters (scale1=scale2=shape1=shape2=1) give the unit exponential distributions.

**Usage**

```
simu.Frank(n,alpha,scale1=1,scale2=1,shape1=1,shape2=1)
```

**Arguments**

n	sample size
alpha	association (copula) parameter
scale1	scale parameter for X
scale2	scale parameter for Y
shape1	shape parameter for X
shape2	shape parameter for Y

**Details**

See Section 2.6 of Emura et al.(2019) for copulas and bivariate survival times.

**Value**

U	uniformly distributed on (0,1)
V	uniformly distributed on (0,1)
X	Weibull distributed (scale1, shape1)
Y	Weibull distributed (scale2, shape2)

**Author(s)**

Takeshi Emura

## References

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Emura T, Matsui S, Rondeau V (2019), *Survival Analysis with Correlated Endpoints, Joint Frailty-Copula Models*, JSS Research Series in Statistics, Springer

## Examples

```
n=100
Dat=simu.Frank(n=n,alpha=10,scale1=1,scale2=2,shape1=0.5,shape2=2)
plot(Dat[,"U"],Dat[,"V"])
cor(Dat[,"U"],Dat[,"V"],method="kendall")
plot(Dat[,"X"],Dat[,"Y"])
cor(Dat[,"X"],Dat[,"Y"],method="kendall")
```

---

simu.Gumbel

*Simulating data from the Gumbel copula*

---

## Description

n pairs of (U,V) are generated from the Gumbel copula. n paris of (X,Y) are generated from the corresponding bivariate survival model with the Weibull marginal distributions. The default parameters (scale1=scale2=shape1=shape2=1) give the unit exponential distributions.

## Usage

```
simu.Gumbel(n,alpha,scale1=1,scale2=1,shape1=1,shape2=1)
```

## Arguments

n	sample size
alpha	association (copula) parameter
scale1	scale parameter for X
scale2	scale parameter for Y
shape1	shape parameter for X
shape2	shape parameter for Y

## Details

See Section 2.6 of Emura et al.(2019) for copulas and bivariate survival times.

## Value

U	uniformly distributed on (0,1)
V	uniformly distributed on (0,1)
X	Weibull distributed (scale1, shape1)
Y	Weibull distributed (scale2, shape2)

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Emura T, Matsui S, Rondeau V (2019), *Survival Analysis with Correlated Endpoints, Joint Frailty-Copula Models*, JSS Research Series in Statistics, Springer

**Examples**

```
n=100
Dat=simu.Gumbel(n=n,alpha=1,scale1=1,scale2=2,shape1=0.5,shape2=2)
plot(Dat[,"U"],Dat[,"V"])
cor(Dat[,"U"],Dat[,"V"],method="kendall")
plot(Dat[,"X"],Dat[,"Y"])
cor(Dat[,"X"],Dat[,"Y"],method="kendall")
```

---

 Test.Clayton

*A goodness-of-fit test for the Clayton copula*


---

**Description**

Perform a goodness-of-fit test for the Clayton copula based on Emura, Lin and Wang (2010). The test is asymptotically equivalent to the test of Shih (1998).

**Usage**

```
Test.Clayton(x.obs,y.obs,dx,dy,lower=0.001,upper=50,U.plot=TRUE)
```

**Arguments**

x.obs	censored times for X
y.obs	censored times for Y
dx	censoring indicators for X
dy	censoring indicators for Y
lower	lower bound for the association parameter
upper	upper bound for the association parameter
U.plot	if TRUE, draw the plot of $U_{-1}(\theta)$

**Details**

See the references.



**Value**

theta1	association parameter by the pseudo-likelihood estimator
theta2	association parameter by the unweighted estimator
Stat	$\log(\theta_1) - \log(\theta_2)$
Z	Z-value of the goodness-of-fit for the Clayton copula
P	P-value of the goodness-of-fit for the Clayton copula

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

Shih JH (1998) A goodness-of-fit test for association in a bivariate survival model. *Biometrika* 85: 189-200

**Examples**

```
n=20
theta_true=2 ## association parameter ##
r1_true=2 ## hazard for X
r2_true=2 ## hazard for Y

set.seed(1)
V1=runif(n)
V2=runif(n)
X=-1/r1_true*log(1-V1)
W=(1-V1)^(-theta_true)
Y=1/theta_true/r2_true*log( 1-W+W*(1-V2)^(-theta_true/(theta_true+1)) )
C=runif(n,min=0,max=5)

x.obs=pmin(X,C)
y.obs=pmin(Y,C)
dx=X<=C
dy=Y<=C

Test.Clayton(x.obs,y.obs,dx,dy)
```

---

Test.Gumbel

*A goodness-of-fit test for the Gumbel copula*

---

**Description**

Perform a goodness-of-fit test for the Gumbel copula based on Emura, Lin and Wang (2010).



---

U1.Clayton

*Estimation of an association parameter via the pseudo-likelihood*


---

**Description**

Estimate the association parameter of the Clayton copula using bivariate survival data. The estimator was derived by Clayton (1978) and reformulated by Emura, Lin and Wang (2010).

**Usage**

```
U1.Clayton(x.obs,y.obs,dx,dy,lower=0.001,upper=50,U.plot=TRUE)
```

**Arguments**

x.obs	censored times for X
y.obs	censored times for Y
dx	censoring indicators for X
dy	censoring indicators for Y
lower	lower bound for the association parameter
upper	upper bound for the association parameter
U.plot	if TRUE, draw the plot of $U_1(\theta)$

**Details**

Details are seen from the references.

**Value**

theta	association parameter
tau	Kendall's tau ( $=\theta/(\theta+2)$ )

**Author(s)**

Takeshi Emura

**References**

Clayton DG (1978). A model for association in bivariate life tables and its application to epidemiological studies of familial tendency in chronic disease incidence. *Biometrika* 65: 141-51.

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

**Examples**

```

n=200
theta_true=2 ## association parameter ##
r1_true=1 ## hazard for X
r2_true=1 ## hazard for Y

set.seed(1)
V1=runif(n)
V2=runif(n)
X=-1/r1_true*log(1-V1)
W=(1-V1)^(-theta_true)
Y=1/theta_true/r2_true*log( 1-W+W*(1-V2)^(-theta_true/(theta_true+1)) )
C=runif(n,min=0,max=5)

x.obs=pmin(X,C)
y.obs=pmin(Y,C)
dx=X<=C
dy=Y<=C

U1.Clayton(x.obs,y.obs,dx,dy)

```

---

U1.Gumbel

*Estimation of an association parameter via the unweighted estimator*


---

**Description**

Estimate the association parameter of the Gumbel copula using bivariate survival data. The estimator was derived by Emura, Lin and Wang (2010).

**Usage**

```
U1.Gumbel(x.obs,y.obs,dx,dy,lower=0.01,upper=50,U.plot=TRUE)
```

**Arguments**

x.obs	censored times for X
y.obs	censored times for Y
dx	censoring indicators for X
dy	censoring indicators for Y
lower	lower bound for the association parameter
upper	upper bound for the association parameter
U.plot	if TRUE, draw the plot of $U_1(\theta)$

**Details**

Details are seen from the references.

**Value**

theta	association parameter
tau	Kendall's tau ( $=\text{theta}/(\text{theta}+2)$ )

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

**Examples**

```
x.obs=c(1,2,3,4,5,6,7,8,9,10,11,12,13,14,15)
y.obs=c(2,1,4,5,6,8,3,7,10,9,11,12,13,14,15)
dx=c(1,1,1,1,1,1,1,1,1,1,1,1,1,1,1)
dy=c(1,1,1,1,1,1,1,1,1,1,1,1,1,1,1)
U1.Gumbel(x.obs,y.obs,dx,dy)
```

U2.Clayton

*Estimation of an association parameter via the unweighted estimator***Description**

Estimate the association parameter of the Clayton copula using bivariate survival data. The estimator was defined as the unweighted estimator in Emura, Lin and Wang (2010).

**Usage**

```
U2.Clayton(x.obs,y.obs,dx,dy)
```

**Arguments**

x.obs	censored times for X
y.obs	censored times for Y
dx	censoring indicators for X
dy	censoring indicators for Y

**Details**

Details are seen from the references.

**Value**

theta	association parameter
tau	Kendall's tau ( $=\text{theta}/(\text{theta}+2)$ )

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

**Examples**

```
n=200
theta_true=2 ## association parameter ##
r1_true=1 ## hazard for X
r2_true=1 ## hazard for Y

set.seed(1)
V1=runif(n)
V2=runif(n)
X=-1/r1_true*log(1-V1)
W=(1-V1)^(-theta_true)
Y=1/theta_true/r2_true*log( 1-W+W*(1-V2)^(-theta_true/(theta_true+1)) )
C=runif(n,min=0,max=5)

x.obs=pmin(X,C)
y.obs=pmin(Y,C)
dx=X<=C
dy=Y<=C

U2.Clayton(x.obs,y.obs,dx,dy)
```

---

U2.Gumbel

*Estimation of an association parameter via the pseudo-likelihood*


---

**Description**

Estimate the association parameter of the Gumbel copula using bivariate survival data. The estimator was derived by Emura, Lin and Wang (2010).

**Usage**

```
U2.Gumbel(x.obs,y.obs,dx,dy,lower=0.01,upper=50,U.plot=TRUE)
```

**Arguments**

x.obs	censored times for X
y.obs	censored times for Y
dx	censoring indicators for X

dy	censoring indicators for Y
lower	lower bound for the association parameter
upper	upper bound for the association parameter
U.plot	if TRUE, draw the plot of $U_1(\theta)$

**Details**

Details are seen from the references.

**Value**

theta	association parameter
tau	Kendall's tau ( $=\theta/(\theta+1)$ )

**Author(s)**

Takeshi Emura

**References**

Emura T, Lin CW, Wang W (2010) A goodness-of-fit test for Archimedean copula models in the presence of right censoring, *Compt Stat Data Anal* 54: 3033-43

**Examples**

```
x.obs=c(1,2,3,4,5)
y.obs=c(2,1,4,5,6)
dx=c(1,1,1,1,1)
dy=c(1,1,1,1,1)
U2.Gumbel(x.obs,y.obs,dx,dy)
```

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