

Package ‘dae’

April 29, 2015

Version 2.7-0

Date 2015-04-29

Title Functions Useful in the Design and ANOVA of Experiments

Author Chris Brien <Chris.Brien@unisa.edu.au>.

Maintainer Chris Brien <Chris.Brien@unisa.edu.au>

Depends R (>= 2.10.0), ggplot2, methods

Description The content falls into the following groupings: (i) Data, (ii) Factor manipulation functions, (iii) Design functions, (iv) ANOVA functions, (v) Matrix functions, (vi) Projector and canonical efficiency functions, and (vii) Miscellaneous functions. A document 'daeDesignRandomization.pdf', available in the doc subdirectory of the installation directory for 'dae', describes the use of the package for generating randomized layouts for experiments. The ANOVA functions facilitate the extraction of information when the 'Error' function has been used in the call to 'aov'.

License GPL (>=2)

URL <http://chris.brien.name>

NeedsCompilation no

R topics documented:

dae-package	3
ABC.Interact.dat	6
as.numfac	6
blockboundary.plot	7
correct.degfree	8
decomp.relate	9
degfree	11
design.plot	12
efficiencies.p2canon	14
efficiencies.pcanon	15
efficiency.criteria	16
elements	17
extab	18
fac.ar1mat	19
fac.combine	20

fac.divide	21
fac.gen	22
fac.layout	23
fac.match	25
fac.meanop	26
fac.nested	27
fac.recode	28
fac.sumop	29
fac.vcmat	30
Fac4Proc.dat	31
fitted.aovlist	31
fitted.errors	32
get.daeTolerance	33
harmonic.mean	34
interaction.ABC.plot	35
is.allzero	36
is.projector	37
mat.ar1	38
mat.banded	39
mat.dirprod	39
mat.dirsum	40
mat.exp	41
mat.I	41
mat.J	42
meanop	42
mpone	43
no.reps	44
power.exp	45
print.projector	46
print.summary.p2canon	46
print.summary.pcanon	47
proj2.combine	48
proj2.decomp	50
proj2.efficiency	50
proj2.eigen	51
proj2.ops	52
projector	53
projector-class	54
projs.2canon	55
projs.canon	57
projs.combine.p2canon	58
projs.structure	59
qqyeffects	61
resid.errors	62
residuals.aovlist	63
rmvnorm	64
Sensory3Phase.dat	65
set.daeTolerance	66
show-methods	67
SPLGrass.dat	68
strength	68
summary.p2canon	69

summary.pcanon	70
tukey.lfd	72
yates.effects	73

Index	75
--------------	-----------

Description

The content falls into the following natural groupings: (i) Data, (ii) Factor manipulation functions, (iii) Design functions, (iv) ANOVA functions, (v) Matrix functions, (vi) Projector and canonical efficiency functions, and (vii) Miscellaneous functions. The document 'daeDesignRandomization.pdf', available in the doc subdirectory of the installation directory for 'dae', describes the use of the package for generating randomized layouts for experiments. The ANOVA functions facilitate the extraction of information when the 'Error' function has been used in the call to 'aov'.

Details

```

Package:    dae
Version:    2.7-0
Date:       2015-04-29
Depends:    R (>= 2.10.0), ggplot2, methods
License:    GPL (>=2)
URL:        http://chris.brien.name
Built:      R 3.1.0; 2015-04-09 UTC; windows

```

Index:

(i) Data

ABC.Interact.dat	Randomly generated set of values indexed by three factors
Fac4Proc.dat	Data for a 2 ⁴ factorial experiment
Sensory3Phase.dat	Data for the three-pahse sensory evaluation experiment in Brien, C.J. and Payne, R.W. (1999)
SPLGrass.dat	Data for an experiment to investigate the effects of grazing patterns on pasture composition

(ii) Factor manipulation functions

as.numfac	Convert a factor to a numeric vector
fac.combine	Combines several factors into one
fac.divide	Divides a factor into several individual factors
fac.gen	Generate all combinations of several factors
fac.match	Match, for each combination of a set of columns in 'x', the row that has the same combination

	in 'table'
fac.nested	creates a factor whose values are generated within those of the factor nesting.fac
fac.recode	Recodes the 'levels' and values of a factor using the value in position i of the 'newlevels' vector to replace the ith 'level' of the 'factor'.
mpone	Converts the first two levels of a factor into the numeric values -1 and +1

(iii) Design functions

blockboundary.plot	This function plots a block boundary on a plot produced by 'design.plot'.
design.plot	This function plots treatments within a matrix.
fac.layout	Generate a randomized layout for an experiment
no.reps	Computes the number of replicates for an experiment
power.exp	Computes the power for an experiment

(iv) ANOVA functions

fitted.aovlist	Extract the fitted values for a fitted model from an aovlist object
fitted.errors	Extract the fitted values for a fitted model
interaction.ABC.plot	Plots an interaction plot for three factors
qqyeffects	Half or full normal plot of Yates effects
resid.errors	Extract the residuals for a fitted model
residuals.aovlist	Extract the residuals from an aovlist object
strength	Generate paper strength values
tukey.1df	Performs Tukey's one-degree-of-freedom-test-for-nonadditivity
yates.effects	Extract Yates effects

(v) Matrix functions

elements	Extract the elements of an array specified by the subscripts
fac.ar1mat	forms the ar1 correlation matrix for a (generalized) factor
fac.sumop	computes the summation matrix that produces sums corresponding to a factor
fac.vcmat	forms the variance matrix for the variance component of a (generalized) factor
mat.I	Forms a unit matrix
mat.J	Forms a square matrix of ones
mat.ar1	Forms an ar1 correlation matrix
mat.dirprod	Forms the direct product of two matrices
mat.dirsum	Forms the direct sum of a list of matrices

(vi) Projector and canonical efficiency functions

correct.degfree	Check the degrees of freedom in an object of class projector
decomp.relate	Examines the relationship between the eigenvectors for two decompositions
degfree	Degrees of freedom extraction and replacement
efficiencies.pcanon	Extracts the canonical efficiency factors from a list of class 'pcanon'
efficiencies.p2canon	Extracts the canonical efficiency factors from a list of class 'p2canon'.
efficiency.criteria	Computes efficiency criteria from a set of efficiency factors
fac.meanop	computes the projection matrix that produces means
is.projector	Tests whether an object is a valid object of class projector
print.projector	Print projectors
proj2.eigen	Canonical efficiency factors and eigenvectors in joint decomposition of two projectors
proj2.efficiency	Computes the canonical efficiency factors for the joint decomposition of two projectors
proj2.combine	Compute the projection and Residual operators for two, possibly nonorthogonal, projectors
projector	Create projectors
projector-class	Class projector
projs.structure	Orthogonalised projectors for the terms in a formula
projs.canon	A canonical analysis of the relationships between two or more sets of projectors
projs.2canon	A canonical analysis of the relationships between two sets of projectors
projs.combine.p2canon	Extract, from a p2canon object, the projectors
print.summary.pcanon	Prints the values in an 'summary.pcanon' object
print.summary.p2canon	Prints the values in an 'summary.p2canon' object that give the combined decomposition
show-methods	Methods for Function show in Package dae
summary.pcanon	A summary of the results of an analysis of the relationships between two or more sets of projectors
summary.p2canon	A summary of the results of an analysis of the relationships between two sets of projectors

(vii) Miscellaneous functions

extab	Expands the values in table to a vector
get.daeTolerance	Gets the value of daeTolerance for the package dae
harmonic.mean	Calculates the harmonic mean.
is.allzero	Tests whether all elements are approximately zero
rmvnorm	generates a vector of random values from a multivariate normal distribution
set.daeTolerance	Sets the value of daeTolerance for the package

dae

Author(s)

Chris Brien <Chris.Brien@unisa.edu.au>.

Maintainer: Chris Brien <Chris.Brien@unisa.edu.au>

ABC.Interact.dat

*Randomly generated set of values indexed by three factors***Description**

This data set has randomly generated values of the response variable MOE (Measure Of Effectiveness) which is indexed by the two-level factors A, B and C.

Usage

```
data(ABC.Interact.dat)
```

Format

A data.frame containing 8 observations of 4 variables.

Source

Generated by Chris Brien

as.numfac

*Convert a factor to a numeric vector***Description**

Converts a [factor](#) to a numeric vector with approximately the numeric values of its levels. Hence, the levels of the [factor](#) must be numeric values, stored as characters. It uses the method described in [factor](#). Use [as.numeric](#) to convert the [factor](#) to a numeric vector with integers 1, 2, ... corresponding to the positions in the list of levels. You can also use [fac.recode](#) to recode the levels to numeric values. If the a numeric is supplied, it is left unchanged.

Usage

```
as.numfac(factor)
```

Arguments

factor The [factor](#) to be converted.

Value

A numeric vector. An NA will be stored for any value of the factor whose level is not a number.

Author(s)

Chris Brien

See Also[as.numeric](#), [fac.recode](#) in package **dae**, [factor](#).**Examples**

```
## set up a factor and convert it to a numeric vector
a <- factor(rep(1:3, 4))
x <- as.numfac(a)
```

blockboundary.plot	<i>This function plots a block boundary on a plot produced by design.plot.</i>
--------------------	--

Description

This function plots a block boundary on a plot produced by [design.plot](#). It allows control of the starting unit, through `rstart` and `cstart`, and the number of rows (`nr`) and columns (`nc`) from the starting unit that the blocks to be plotted are to cover.

Usage

```
blockboundary.plot(bdef = NULL, bseq = FALSE, rstart= 0, cstart = 0,
                  nr, nc, bcol = 1, bwd = 2)
```

Arguments

bdef	<p>A matrix of block sizes:</p> <ul style="list-style-type: none"> • if there is only one row, then the first element is interpreted as the no. rows in each block and blocks with this number of rows are to be repeated across the rows of the design. • if there is more than one row, then each row of the matrix specifies a block, with the sequence of rows in the matrix specifying a corresponding sequence of blocks down the rows of the design. <p>Similarly, a single value for a column specifies a repetition of blocks of that size across the columns of the design, while several column values specifies a sequence of blocks across the columns of the size specified.</p>
bseq	A logical that determines whether block numbers are repetitions or sequences of block numbers.
rstart	A numeric specifying the row after which the plotting of block boundaries is to start.
cstart	A numeric specifying the column after which the plotting of block boundaries is to start.
nr	A numeric the number of rows (<code>nr</code>), from the starting unit, that the blocks to be plotted are to cover.

nc	A numeric the number of columns (nc), from the starting unit, that the blocks to be plotted are to cover.
bcol	A character string specifying the colour of the block boundary. See Colour specification under the par function.
bwd	A numeric giving the width of the block boundary to be plotted.

Value

no values are returned, but modifications are made to the currently active plot.

See Also

[design.plot](#), [par](#), [DiGger](#)

Examples

```
## Not run:
SPL.Lines.mat <- matrix(as.numfac(Lines), ncol=16, byrow=T)
colnames(SPL.Lines.mat) <- 1:16
rownames(SPL.Lines.mat) <- 1:10
SPL.Lines.mat <- SPL.Lines.mat[10:1, 1:16]
windows()
design.plot(SPL.Lines.mat,trts=1:10,new=TRUE,
           rstr="Rows",cstr="Columns", chtdiv=3, rprop = 1,cprop=1,
           plotbdry = TRUE)
#Plot Mainplot boundaries
blockboundary.plot(bdef = cbind(4,16), rstart = 1, bwd = 3, bcol = "green",
                  nr = 9, nc = 16)
blockboundary.plot(bdef = cbind(1,4), bwd = 3, bcol = "green", nr = 1, nc = 16)
blockboundary.plot(bdef = cbind(1,4), rstart= 9, bwd = 3, bcol = "green",
                  nr = 10, nc = 16)
#Plot all 4 block boundaries
blockboundary.plot(bdef = cbind(8,5,5,4), bseq=T, cstart = 1, rstart= 1,
                  bwd = 3,bcol = "blue", nr = 9, nc = 15)
blockboundary.plot(bdef = cbind(10,16), bwd=3,bcol="blue", nr=10, nc=16)
#Plot border and internal block boundaries only
blockboundary.plot(bdef = cbind(8,14), cstart = 1, rstart= 1,
                  bwd = 3, bcol = "blue", nr = 9, nc = 15)
blockboundary.plot(bdef = cbind(10,16), bwd = 3, bcol = "blue",
                  nr = 10, nc = 16)
## End(Not run)
```

correct.degfree

Check the degrees of freedom in an object of class projector

Description

Check the degrees of freedom in an object of class ["projector"](#).

Usage

```
correct.degfree(object)
```


Arguments

object An object of class "[projector](#)" whose degrees of freedom are to be checked.

Details

The degrees of freedom of the projector are obtained as its number of nonzero eigenvalues. An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

TRUE or FALSE depending on whether the correct degrees of freedom have been stored in the object of class "[projector](#)".

Author(s)

Chris Brien

See Also

[degfree](#), [projector](#) in package **dae**.
[projector](#) for further information about this class.

Examples

```
## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## create a projector based on the matrix m
proj.m <- new("projector", data=m)

## add its degrees of freedom
degfree(proj.m) <- 1

## check degrees of freedom are correct
correct.degfree(proj.m)
```

decomp.relate	<i>Examines the relationship between the eigenvectors for two decompositions</i>
---------------	--

Description

Two decompositions produced by [proj2.eigen](#) are compared by computing all pairs of crossproduct sums of eigenvectors from the two decompositions. It is most useful when the calls to [proj2.eigen](#) have the same Q1.

Usage

```
decomp.relate(decomp1, decomp2)
```

Arguments

decomp1	A list containing components efficiencies and eigenvectors such as is produced by proj2.eigen .
decomp2	Another list containing components efficiencies and eigenvectors such as is produced by proj2.eigen .

Details

Each element of the $r_1 \times r_2$ [matrix](#) is the sum of crossproducts of a pair of eigenvectors, one from each of the two decompositions. A sum is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

A [matrix](#) that is $r_1 \times r_2$ where r_1 and r_2 are the numbers of efficiencies of `decomp1` and `decomp2`, respectively. The rownames and columnnames of the [matrix](#) are the values of the efficiency factors from `decomp1` and `decomp2`, respectively.

Author(s)

Chris Brien

See Also

[proj2.eigen](#), [proj2.combine](#) in package **dae**, [eigen](#).

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

## obtain intra- and inter-block decompositions
decomp.inter <- proj2.eigen(Q.unit[["Block"]], Q.trt[["trt"]])
decomp.intra <- proj2.eigen(Q.unit[["Block:Unit"]], Q.trt[["trt"]])

## check that intra- and inter-block decompositions are orthogonal
decomp.relate(decomp.intra, decomp.inter)
```

degfree

*Degrees of freedom extraction and replacement***Description**

Extracts the degrees of freedom from or replaces them in an object of class "[projector](#)".

Usage

```
degfree(object)
```

```
degfree(object) <- value
```

Arguments

object	An object of class " projector " whose degrees of freedom are to be extracted or replaced.
value	An integer to which the degrees of freedom are to be set or an object of class " projector " or "matrix" from which the degrees of freedom are to be calculated.

Details

There is no checking of the correctness of the degrees of freedom, either already stored or as a supplied integer value. This can be done using [correct.degfree](#).

When the degrees of freedom of the projector are to be calculated, they are obtained as the number of nonzero eigenvalues. An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

An object of class "[projector](#)" that consists of a square, summetric, idempotent matrix and degrees of freedom (rank) of the matrix.

Author(s)

Chris Brien

See Also

[correct.degfree](#), [projector](#) in package **dae**.
[projector](#) for further information about this class.

Examples

```
## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## coerce to a projector
proj.m <- projector(m)

## extract its degrees of freedom
```

```
degfree(proj.m)

## create a projector based on the matrix m
proj.m <- new("projector", data=m)

## add its degrees of freedom and print the projector
degfree(proj.m) <- proj.m
print(proj.m)
```

design.plot

This function plots treatments within a matrix.

Description

This function plots treatments within a matrix and may be used to build a graphical representation of a matrix, highlighting the position of certain treatments and the blocking factors used in the design. It is a modified version of the function supplied with DiGger. It includes more control over the labelling of the rows and columns of the design and allows for more flexible plotting of designs with unequal block size.

Usage

```
design.plot(dsgn, trts = NULL, rprop = 1, cprop = 1, label = TRUE,
           plotchar = NULL, plotbdry = TRUE, chtdiv = 2,
           bseq = FALSE, bdef = NULL, bcol = 1, bwd = 2,
           rotate = FALSE, new = TRUE,
           cstr = "Range", rstr = "Row", rlab = TRUE, clab = TRUE,
           font = 1, rdecrease = FALSE, cdecrease = FALSE, ...)
```

Arguments

dsgn	a matrix containing a set of integers or characters representing the treatments.
trts	A integer or character vector giving specific treatment labels to be plotted.
rprop	a value giving the proportion of the row boundary of cell to plot.
cprow	a value giving the proportion of the column boundary of cell to plot.
label	a logical to indicate whether treatment labels are to be plotted in the cells. If TRUE, print a label for all treatments or specific treatments listed in trts. If FALSE, no labels are not printed in the cells.
plotchar	Either a character vector containing labels for the whole set of treatments or a single integer specifying a symbol to be used in plotting treatments.
plotbdry	A logical indicting whether a boundary is to plotted around a cell.
chtdiv	A numeric specifying the amount by which plotting text and symbols should be magnified/reduced relative to the default.
bseq	A logical that determines whether block numbers are repetitions or sequences of block numbers.
bdef	A matrix of block sizes: <ul style="list-style-type: none"> if there is only one row, then the first element is interpreted as the no. rows in each block and blocks with this number of rows are to be repeated across the rows of the design.

- if there is more than one row, then each row of the matrix specifies a block, with the sequence of rows in the matrix specifying a corresponding sequence of blocks down the rows of the design.

Similarly, a single value for a column specifies a repetition of blocks of that size across the columns of the design, while several column values specifies a sequence of blocks across the columns of the size specified.

bcol	A character string specifying the colour of the block boundary. See Colour specification under the par function.
bwd	A numeric giving the width of the block boundary to be plotted.
rotate	A logical which, if TRUE, results in the matrix being rotated 90 degrees for plotting.
new	A logical indicating if a new plot is to be produced or the current plot is added to.
cstr	A character string to use as a label for columns of the matrix .
rstr	A character string to use as a label for rows of the matrix .
rlab	A logical indicating each row of the design is labelled. If the rows of the matrix are labelled, these are used; otherwise 1:nrow is used.
clab	A logical indicating each column of the design is labelled. If the columns of the matrix are labelled, these are used; otherwise 1:ncol is used.
font	An integer specifying the font family to be used for row and column labelling.
rdecrease	A logical indicating whether to reverse the row labels.
cdecrease	A logical indicating whether to reverse the column labels.
...	further arguments passed to polygon in plotting the cell.

Value

no values are returned, but a plot is produced.

References

Coombes, N. E. (2009). *DiGger design search tool in R*. <http://www.austatgen.org/files/software/downloads/>

See Also

[blockboundary.plot](#), [par](#), [polygon](#), [DiGger](#)

Examples

```
## Not run:
design.plot(des.mat, trts=1:4, col="lightblue", new=TRUE,
            rstr="Lanes", cstr="Positions", chtdiv=3, rprop = 1, cprop=1,
            plotbndry = TRUE)
design.plot(des.mat, trts=5:87, label=T, col="grey", chtdiv=3, new=FALSE,
            plotbndry = TRUE)
design.plot(des.mat, trts=88:434, label=T, col="lightgreen", chtdiv=3,
            new=FALSE, plotbndry = TRUE,
            bseq=TRUE, bdef=cbind(4,10,12), bwd=3, bcol="blue")
## End(Not run)
```

efficiencies.p2canon *Extracts the canonical efficiency factors from a list of class p2canon.*

Description

Produces a list containing the canonical efficiency factors for the joint decomposition of two sets of projectors (Brien and Bailey, 2009) obtained using [projs.2canon](#).

Usage

```
efficiencies.p2canon(object, which = "adjusted")
```

Arguments

object	A list of class p2canon produced by projs.2canon .
which	A character string, either adjusted or pairwise. For adjusted, the canonical efficiency factor are adjusted for other projectors from Q2. For pairwise, they are the unadjusted canonical efficiency factors between pairs of projectors consisting of one projector from each of two sets.

Value

A list with a component for each element of the Q1 argument from [projs.2canon](#). Each component is list, each its components corresponding to an element of the Q2 argument from [projs.2canon](#)

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

See Also

[projs.2canon](#), [summary.p2canon](#), [proj2.efficiency](#), [proj2.combine](#), [proj2.eigen](#), [projs.structure](#) in package **dae**, [eigen](#).
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain projectors using projs.structure
```

```
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition and summarize
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
efficiencies.p2canon(unit.trt.p2canon)
```

efficiencies.pcanon *Extracts the canonical efficiency factors from a list of class pcanon.*

Description

Produces a list containing the canonical efficiency factors for the joint decomposition of two or more sets of projectors (Brien and Bailey, 2009) obtained using [projs.canon](#).

Usage

```
efficiencies.pcanon(object, which = "adjusted")
```

Arguments

object	A list of class pcanon produced by projs.canon .
which	A character string, either adjusted or pairwise. For adjusted, the canonical efficiency factor are adjusted for other projectors from from the same set. For pairwise, they are the unadjusted canonical efficiency factors between pairs of projectors consisting of one projector from each of two sets.

Value

A list with a component for each component of object, except for the last component – [projs.canon](#) for more information about the components of a pcanon object.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

See Also

[projs.canon](#), [summary.pcanon](#), [proj2.efficiency](#), [proj2.combine](#), [proj2.eigen](#), [projs.structure](#) in package **dae**, [eigen](#).

[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain combined decomposition and summarize
unit.trt.canon <- projs.canon(list(unit=~ Block/Unit, trt=~ trt), data = PBIBD2.lay)
efficiencies.pcanon(unit.trt.canon)
```

efficiency.criteria *Computes efficiency criteria from a set of efficiency factors*

Description

Computes efficiency criteria from a set of efficiency factors.

Usage

```
efficiency.criteria(efficiencies)
```

Arguments

efficiencies A numeric containing a set of efficiency factors.

Details

The aefficiency criterion is the harmonic mean of the efficiency factors. The mefficiency criterion is the mean of the efficiency factors. The eefficiency criterion is the minimum of the efficiency factors. The sefficiency criterion is the variance of the efficiency factors. The order is the order of balance and is the number of unique efficiency factors.

Value

A list whose components are aefficiency, mefficiency, eefficiency, sefficiency and order.

Author(s)

Chris Brien

See Also

[proj2.efficiency](#), [proj2.eigen](#), [proj2.combine](#) in package **dae**, **eigen**.
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

## save intrablock efficiencies
eff.inter <- proj2.efficiency(Q.unit[["Block:Unit"]], Q.trt[["trt"]])

## calculate efficiency criteria
efficiency.criteria(eff.inter)
```

elements

Extract the elements of an array specified by the subscripts

Description

Elements of the array `x` corresponding to the rows of the two dimensional object `subscripts` are extracted. The number of columns of `subscripts` corresponds to the number of dimensions of `x`. The effect of supplying less columns in `subscripts` than the number of dimensions in `x` is the same as for `"["`.

Usage

```
elements(x, subscripts)
```

Arguments

<code>x</code>	An array with at least two dimensions whose elements are to be extracted.
<code>subscripts</code>	A two dimensional object interpreted as elements by dimensions.

Value

A vector containing the extracted elements and whose length equals the number of rows in the `subscripts` object.

See Also

Extract

Examples

```
## Form a table of the means for all combinations of Row and Line.
## Then obtain the values corresponding to the combinations in the data frame x,
## excluding Row 3.
x <- fac.gen(list(Row = 2, Line = 4), each = 2)
x$y <- rnorm(16)
RowLine.tab <- tapply(x$y, list(x$Row, x$Line), mean)
xs <- elements(RowLine.tab, subscripts=x[x$"Line" != 3, c("Row", "Line")])
```

extab	<i>Expands the values in table to a vector</i>
-------	--

Description

Expands the values in table to a vector according to the `index.factors` that are considered to index the table, either in standard or Yates order. The order of the values in the vector is determined by the order of the values of the `index.factors`.

Usage

```
extab(table, index.factors, order="standard")
```

Arguments

table	A numeric vector containing the values to be expanded. Its length must equal the product of the number of used levels for the <code>index.factors</code> and the values in it correspond to all levels combinations of these <code>index.factors</code> . That is, the values of the <code>index.factors</code> are irrelevant to table.
index.factors	A list of <code>index.factors</code> that index the table. All the <code>index.factors</code> must be the same length.
order	The order in which the levels combinations of the <code>index.factors</code> are to be considered as numbered in indexing table; standard numbers them as if they are arranged in standard order, that is with the first factor moving slowest and the last factor moving fastest; yates numbers them as if they are arranged in Yates order, that is with the first factor moving fastest and last factor moving slowest.

Value

A vector of length equal to the `index.factors` whose values are taken from table.

Author(s)

Chris Brien

Examples

```
## generate a small completely randomized design with the two-level
## factors A and B
n <- 12
CRD.unit <- list(Unit = n)
CRD.treat <- fac.gen(list(A = 2, B = 2), each = 3)
CRD.lay <- fac.layout(unrandomized=CRD.unit, randomized=CRD.treat,
                      seed=956)

## set up a 2 x 2 table of A x B effects
AB.tab <- c(12, -12, -12, 12)

## add a unit-length vector of expanded effects to CRD.lay
attach(CRD.lay)
CRD.lay$AB.effects <- extab(table=AB.tab, index.factors=list(A, B))
```

fac.ar1mat	<i>forms the ar1 correlation matrix for a (generalized) factor</i>
------------	--

Description

Form the correlation matrix for a (generalized) factor where the correlation between the levels follows an autocorrelation of order 1 (ar1) pattern.

Usage

```
fac.ar1mat(factor, rho)
```

Arguments

factor	The (generalized) factor for which the correlation between its levels displays an ar1 pattern.
rho	The correlation parameter for the ar1 process.

Details

The method is: a) form an $n \times n$ matrix of all pairwise differences in the numeric values corresponding to the observed levels of the factor by taking the difference between the following two $n \times n$ matrices are equal: 1) each row contains the numeric values corresponding to the observed levels of the factor, and 2) each column contains the numeric values corresponding to the observed levels of the factor, b) replace each element of the pairwise difference matrix with ρ raised to the absolute value of the difference.

Value

An $n \times n$ [matrix](#), where n is the length of the [factor](#).

Author(s)

Chris Brien

See Also

`fac.vcmat`, `fac.meanop`, `fac.sumop` in package **dae**.

Examples

```
## set up a two-level factor and a three-level factor, both of length 12
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## create a 12 x 12 ar1 matrix corresponding to B
ar1.B <- fac.ar1mat(B, 0.6)
```

fac.combine

Combines several factors into one

Description

Combines several **factors** into one whose levels are the combinations of the used levels of the individual **factors**.

Usage

```
fac.combine(factors, order="standard", combine.levels=FALSE, sep=",", ...)
```

Arguments

factors	A list of factors all of the same length.
order	Either standard or yates. The order in which the levels combinations of the factors are to be considered as numbered when forming the levels of the combined factor ; standard numbers them as if they are arranged in standard order, that is with the levels of the first factor moving slowest and those of the last factor moving fastest; yates numbers them as if they are arranged in Yates order, that is with the levels of the first factor moving fastest and those of the last factor moving slowest.
combine.levels	A logical specifying whether the levels labels of the new factor are to be combined from those of the factors being combined. The default is to use the integers from 1 to the product of the numbers of combinations of used levels of the individual factors , numbering the levels according to order.
sep	A character string to separate the levels when combine.levels = TRUE.
...	Further arguments passed to the factor call creating the new factor .

Value

A **factor** whose levels are formed from the observed combinations of the levels of the individual **factors**.

Author(s)

Chris Brien

See Also

`fac.divide` in package **dae**.

Examples

```
## set up two factors
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## obtain six-level factor corresponding to the combinations of A and B
AB <- fac.combine(list(A,B))
```

fac.divide	<i>Divides a factor into several individual factors</i>
------------	---

Description

Takes a **factor** and divides it into several individual **factors** as if the levels in the original **factor** correspond to the numbering of the levels combinations of the individual **factors** when these are arranged in standard or Yates order.

Usage

```
fac.divide(combined.factor, factor.names, order="standard")
```

Arguments

combined.factor	A factor that is to be divided into the individual factors listed in <code>factor.names</code> .
factor.names	A list of factors to be formed. The names in the list are the names of the factors and the component of a name is either a) a single numeric value that is the number of levels, b) a numeric vector that contains the levels of the factor , or c) a character vector that contains the labels of the levels of the factor .
order	Either standard or yates. The order in which the levels combinations of the factors in <code>factor.names</code> are to be considered as numbered; standard numbers them as if they are arranged in standard order, that is with the first factor moving slowest and the last factor moving fastest; yates numbers them as if they are arranged in Yates order, that is with the first factor moving fastest and last factor moving slowest.

Value

A **data.frame** whose columns consist of the **factors** listed in `factor.names` and whose values have been computed from the combined **factor**. All the **factors** will be of the same length.

Note

A single **factor** name may be supplied in the **list** in which case a **data.frame** is produced that contains the single **factor** computed from the numeric vector. This may be useful when calling this function from others.

Author(s)

Chris Brien

See Also[fac.combine](#) in package **dae**.**Examples**

```
## generate a small completely randomized design for 6 treatments
n <- 12
CRD.unit <- list(Unit = n)
treat <- factor(rep(1:4, each = 3))
CRD.lay <- fac.layout(unrandomized=CRD.unit, randomized=treat, seed=956)

## divide the treatments into two two-level factor A nd B
CRD.facs <- fac.divide(CRD.lay$treat, factor.names = list(A = 2, B = 2))
```

fac.gen

*Generate all combinations of several factors***Description**

Generate all combinations of several factors.

Usage

```
fac.gen(generate, each=1, times=1, order="standard")
```

Arguments

generate	A list of named objects and numbers that specify the factors whose levels are to be generated and the pattern in these levels. If a component of the list is named, then the component should be either a) a single numeric value that is the number of levels, b) a numeric vector that contains the levels of the factor , or c) a character vector that contains the labels of the levels of the factor .
each	The number of times to replicate consecutively the elements of the levels generated according to pattern specified by the generate argument.
times	The number of times to repeat the whole generated pattern of levels generated according to pattern specified by the generate argument.
order	Either standard or yates. The order in which the speed of cycling through the levels is to move; combinations of the factors are to be considered as numbered; standard cycles through the levels of the first factor slowest and the last factor moving fastest; yates cycles through the levels of the first factor fastest and last factor moving slowest.

Details

The levels of each **factor** are generated in a hierarchical pattern where the levels of one **factor** are held constant while those of the adjacent **factor** are cycled through the complete set once. If a number is supplied instead of a name, the pattern is generated as if a **factor** with that number of levels had been supplied in the same position as the number. However, no levels are stored for this unnamed **factor**.

Value

A **data.frame** of generated levels with columns corresponding to the codefactors in the generate list.

Warning

Avoid using factor names F and T as these might be confused with FALSE and TRUE.

Author(s)

Chris Brien

See Also

fac.combine in package **dae**

Examples

```
## generate a 2^3 factorial experiment with levels - and +, and
## in Yates order
mp <- c("-", "+")
fnames <- list(Catal = mp, Temp = mp, Press = mp, Conc = mp)
Fac4Proc.Treats <- fac.gen(generate = fnames, order="yates")

## Generate the factors A, B and D. The basic pattern has 4 repetitions
## of the levels of D for each A and B combination and 3 repetitions of
## the pattern of the B and D combinations for each level of A. This basic
## pattern has each combination repeated twice, and the whole of this
## is repeated twice. It generates 864 A, B and D combinations.
gen <- list(A = 3, 3, B = c(0,100,200), 4, D = c("0","1"))
fac.gen(gen, times=2, each=2)
```

fac.layout

Generate a randomized layout for an experiment

Description

Generate a layout for an experiment consisting of randomized **factors** that are randomized to the unrandomized **factors**, taking into account the nesting, for the design, between the unrandomized factors.

Usage

```
fac.layout(unrandomized, nested.factors=NULL, randomized,
           seed=NULL, unit.permutation=TRUE)
```

Arguments

- unrandomized A `data.frame` or a `list` of `factors`, along with their levels. If a `list`, the name of each component of the `list` is a `factor` name and the component is either a single numeric value that is the number of levels, a numeric vector that contains the levels of the `factor` or a character codevector that contains the labels of the levels of the `factor`.
- nested.factors A `list` of the unrandomized `factors` that are nested in other `factors` in unrandomized. The name of each component is the name of a `factor` that is nested and the component is a character vector containing the `factors` within which it is nested. It is emphasized that the nesting is a property of the design that is being employed (it is only partly based on the intrinsic nesting).
- randomized A `factor` or a `data.frame` containing the values of the `factor`(s) to be randomized.
- seed A single value, interpreted as an integer, that specifies the starting value of the random number generator.
- unit.permutation A logical indicating whether to include the `.Unit` and `.Permutation` columns in the `data.frame`.

Details

This function uses the method of randomization described by Bailey (1981). That is, a permutation of the units that respects the nesting for the design is obtained. This permutation is applied jointly to the unrandomized and randomized `factors` to produce the randomized layout. The `.Units` and `.Permutation` vectors enable one to swap between this permutation and the randomized layout. The i th value in `.Permutation` gives the unit to which unit i was assigned in the randomization.

Value

A `data.frame` consisting of the values for `.Units` and `.Permutation` vectors, provided `unit.permutation` is TRUE, along with the values for the unrandomized and randomized `factors` that specify the randomized layout for the experiment.

Author(s)

Chris Brien

References

Bailey, R.A. (1981) A unified approach to design of experiments. *Journal of the Royal Statistical Society, Series A*, **144**, 214–223.

See Also

`fac.gen` in package `dae`.

Examples

```
## generate a randomized layout for a 4 x 4 Latin square
## (the nested.factors argument is not needed here as none of the
## factors are nested)
LS.unit <- data.frame(row = ordered(rep(c("I","II","III","IV"), times=4)),
```



```

col = factor(rep(c(0,2,4,6), each=4)))
LS.ran <- data.frame(treat = factor(c(1:4, 2,3,4,1, 3,4,1,2, 4,1,2,3)))
data.frame(LS.unit, LS.ran)
LS.lay <- fac.layout(unrandomized=LS.unit, randomized=LS.ran, seed=7197132)
LS.lay[LS.lay$.Permutation,]

## generate a randomized layout for a replicated randomized complete
## block design, with the block factors arranged in standard order for
## rep then plot and then block
RCBD.unit <- list(rep = 2, plot=1:3, block = c("I","II"))
## specify that plot is nested in block and rep and that block is nested
## in rep
RCBD.nest <- list(plot = c("block","rep"), block="rep")
## generate treatment factor in systematic order so that they correspond
## to plot
tr <- factor(rep(1:3, each=2, times=2))
## obtain randomized layout
RCBD.lay <- fac.layout(unrandomized=RCBD.unit,
                      nested.factors=RCBD.nest,
                      randomized=tr, seed=9719532)
#sort into the original standard order
RCBD.perm <- RCBD.lay[RCBD.lay$.Permutation,]
#resort into randomized order
RCBD.lay <- RCBD.perm[order(RCBD.perm$.Units),]

## generate a layout for a split-unit experiment in which:
## - the main-unit factor is A with 4 levels arranged in
##   a randomized complete block design with 2 blocks;
## - the split-unit factor is B with 3 levels.
SPL.lay <- fac.layout(unrandomized=list(block = 2, main.unit = 4, split.unit = 3),
                    nested.factors=list(main.unit = "block",
                                         split.unit = c("block", "main.unit")),
                    randomized=fac.gen(list(A = 4, B = 3), times = 2),
                    seed=155251978, unit.permutation=FALSE)

```

fac.match

Match, for each combination of a set of columns in x, the row that has the same combination in table

Description

Match, for each combination of a set of columns in x, the rows that has the same combination in table. The argument `multiples.allow` controls what happens when there are multiple matches in table of a combination in x.

Usage

```
fac.match(x, table, col.names, nomatch = NA_integer_, multiples.allow = FALSE)
```

Arguments

x	an R object, normally a data.frame, possibly a matrix.
table	an R object, normally a data.frame, possibly a matrix.
col.names	A character vector giving the columns in x and table that are to be matched.

nomatch The value to be returned in the case when no match is found. Note that it is coerced to integer.

multiples.allow A logical indicating whether multiple matches of a combination in `x` to those in `table` is allowed. If `multiples.allow` is `FALSE`, an error is generated. If `multiples.allow` is `TRUE`, the first occurrence in `table` is matched. This function can be viewed as a generalization to multiple vectors of the [match](#) function that applies to single vectors.

Value

A [vector](#) of length equal to `x` that gives the rows in `table` that match the combinations of `col.names` in `x`. The order of the rows is the same as the order of the combinations in `x`. The value returned if a combination is unmatched is specified in the `nomatch` argument.

Author(s)

Chris Brien

See Also

[match](#)

Examples

```
## Not run:
#A single unmatched combination
kdata <- data.frame(Expt="D197-5",
                   Row=8,
                   Column=20, stringsAsFactors=FALSE)
index <- fac.match(kdata, D197.dat, c("Expt", "Row", "Column"))

# A matched and an unmatched combination
kdata <- data.frame(Expt=c("D197-5", "D197-4"),
                   Row=c(8, 10),
                   Column=c(20, 8), stringsAsFactors=FALSE)
index <- fac.match(kdata, D197.dat, c("Expt", "Row", "Column"))

## End(Not run)
```

fac.meanop

computes the projection matrix that produces means

Description

Computes the symmetric projection matrix that produces the means corresponding to a (generalized) [factor](#).

Usage

```
fac.meanop(factor)
```

Arguments

factor The (generalized) [factor](#) whose means the projection matrix computes from an observation-length vector.

Details

The design matrix **X** for a (generalized) [factor](#) is formed with a column for each level of the (generalized) [factor](#), this column being its indicator variable. The projection matrix is formed as $X \%*\% (1/\text{diag}(r) \%*\% t(X))$, where *r* is the vector of levels replications.

A generalized [factor](#) is a [factor](#) formed from the combinations of the levels of several original [factors](#). Generalized [factors](#) can be formed using [fac.combine](#).

Value

A [projector](#) containing the symmetric, projection matrix and its degrees of freedom.

Author(s)

Chris Brien

See Also

[fac.combine](#), [projector](#), [degfree](#), [correct.degfree](#), [fac.sumop](#) in package **dae**.
[projector](#) for further information about this class.

Examples

```
## set up a two-level factor and a three-level factor, both of length 12
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## create a generalized factor whose levels are the combinations of A and B
AB <- fac.combine(list(A,B))

## obtain the operator that computes the AB means from a vector of length 12
M.AB <- fac.meanop(AB)
```

fac.nested	<i>creates a factor whose values are generated within those of the factor nesting.fac</i>
------------	---

Description

Creates a [factor](#) whose levels are generated within those of the factor `nesting.fac`. All elements of `nesting.fac` having the same level are numbered from 1 to the number of different elements having that level.

Usage

```
fac.nested(nesting.fac, levels=NA, labels=NA, ...)
```

Arguments

nesting.fac	The factor within each of whose levels the created factor is to be generated.
levels	Optional vector of levels for the factor . Any data value that does not match a value in levels will be NA in the factor . The default value of levels is the the list of numbers from 1 to the maximum replication of the levels of nesting.fac, represented as characters.
labels	Optional vector of values to use as labels for the levels of the factor . The default is as.character(levels).
...	Further arguments passed to the factor call dreating the new factor .

Value

A [factor](#) that is a character vector with class attribute "[factor](#)" and a levels attribute which determines what character strings may be included in the vector.

Note

The levels of nesting.fac do not have to be equally replicated.

Author(s)

Chris Brien

See Also

[fac.gen](#) in package **dae**, [factor](#).

Examples

```
## set up factor A
A <- factor(c(1, 1, 1, 2, 2))

## create nested factor
B <- fac.nested(A)
```

fac.recode	<i>Recodes the levels and values of a factor using the value in position <i>i</i> of the newlevels vector to replace the <i>ith</i> level of the factor.</i>
------------	--

Description

Recodes factor levels using values in a vector. The new levels do not have to be unique.

Usage

```
fac.recode(factor, newlevels, ...)
```

Arguments

factor	The factor to be recoded.
newlevels	A vector of length levels(factor) containing values to use in the recoding.
...	Further arguments passed to the factor call dreating the new factor .

Value

A [factor](#).

Author(s)

Chris Brien

See Also

[as.numfac](#) and [mpone](#) in package **dae**, [factor](#), [relevel](#).

Examples

```
## set up a factor with labels
a <- factor(rep(1:4, 4), labels=c("A","B","C","D"))

## recode "A" and "D" to 1 and "B" and "C" to 2
b <- fac.recode(a, c(1,2,2,1))
```

fac.sumop	<i>computes the summation matrix that produces sums corresponding to a factor</i>
-----------	---

Description

Computes the matrix that produces the sums corresponding to a (generalized) [factor](#).

Usage

```
fac.sumop(factor)
```

Arguments

factor	The (generalized) factor whose sums the summation matrix computes from an observation-length vector.
--------	--

Details

The design matrix **X** for a (generalized) [factor](#) is formed with a column for each level of the (generalized) [factor](#), this column being its indicator variable. The summation matrix is formed as `X %*% t(X)`.

A generalized [factor](#) is a [factor](#) formed from the combinations of the levels of several original [factors](#). Generalized [factors](#) can be formed using [fac.combine](#).

Value

A symmetric matrix.

Author(s)

Chris Brien

See Also

[fac.combine](#), [fac.meanop](#) in package **dae**.

Examples

```
## set up a two-level factor and a three-level factor, both of length 12
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## create a generalized factor whose levels are the combinations of A and B
AB <- fac.combine(list(A,B))

## obtain the operator that computes the AB means from a vector of length 12
S.AB <- fac.sumop(AB)
```

fac.vcmat	<i>forms the variance matrix for the variance component of a (generalized) factor</i>
-----------	---

Description

Form the variance matrix for a (generalized) factor whose effects for its different levels are independently and identically distributed, with their variance given by the variance component; elements of the matrix will equal either zero or sigma2 and displays compound symmetry.

Usage

```
fac.vcmat(factor, sigma2)
```

Arguments

factor	The (generalized) factor for which the variance matrix is required.
sigma2	The variance component, being the of the random effects for the factor.

Details

The method is: a) form the $n \times n$ summation or relationship matrix whose elements are equal to zero except for those elements whose corresponding elements in the following two $n \times n$ matrices are equal: 1) each row contains the numeric values corresponding to the observed levels of the factor, and 2) each column contains the numeric values corresponding to the observed levels of the factor, b) multiply the summation matrix by sigma2.

Value

An $n \times n$ [matrix](#), where n is the length of the [factor](#).

Author(s)

Chris Brien

See Also

[fac.ar1mat](#), [fac.meanop](#), [fac.sumop](#) in package **dae**.

Examples

```
## set up a two-level factor and a three-level factor, both of length 12
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## create a 12 x 12 ar1 matrix corresponding to B
vc.B <- fac.vcmat(B, 2)
```

Fac4Proc.dat

*Data for a 2⁴ factorial experiment***Description**

The data set come from an unreplicated 2⁴ factorial experiment to investigate a chemical process. The response variable is the Conversion percentage (Conv) and this is indexed by the 4 two-level factors Catal, Temp, Press and Conc, with levels “-” and “+”. The data is aranged in Yates order. Also included is the 16-level factor Runs which gives the order in which the combinations of the two-level factors were run.

Usage

```
data(Fac4Proc.dat)
```

Format

A data.frame containing 16 observations of 6 variables.

Source

Table 10.6 of Box, Hunter and Hunter (1978) *Statistics for Experimenters*. New York, Wiley.

fitted.aovlist

*Extract the fitted values for a fitted model from an aovlist object***Description**

Extracts the fitted values as the sum of the effects for all the fitted terms in the model, stopping at `error.term` if this is specified. It is a method for the generic function [fitted](#).

Usage

```
## S3 method for class 'aovlist'
fitted(object, error.term=NULL, ...)
```

Arguments

<code>object</code>	An aovlist object created from a call to aov .
<code>error.term</code>	The term from the Error function down to which effects are extracted for adding to the fitted values. The order of terms is as given in the ANOVA table. If <code>error.term</code> is NULL effects are extracted from all Error terms.
<code>...</code>	Further arguments passed to or from other methods.

Value

A numeric vector of fitted values.

Note

Fitted values will be the sum of effects for terms from the model, but only for terms external to any Error function. If you want effects for terms in the Error function to be included, put them both inside and outside the Error function so they occur twice.

Author(s)

Chris Brien

See Also

[fitted.errors](#), [resid.errors](#), [tukey.1df](#) in package **dae**.

Examples

```
## set up data frame for randomized complete block design in Table 4.4 from
## Box, Hunter and Hunter (2005) Statistics for Experimenters. 2nd edn
## New York, Wiley.
RCBDPen.dat <- fac.gen(list(Blend=5, Flask=4))
RCBDPen.dat$Treat <- factor(rep(c("A","B","C","D"), times=5))
RCBDPen.dat$Yield <- c(89,88,97,94,84,77,92,79,81,87,87,
                      85,87,92,89,84,79,81,80,88)

## perform the analysis of variance
RCBDPen.aov <- aov(Yield ~ Blend + Treat + Error(Blend/Flask), RCBDPen.dat)
summary(RCBDPen.aov)

## two equivalent ways of extracting the fitted values
fit <- fitted.aovlist(RCBDPen.aov)
fit <- fitted(RCBDPen.aov, error.term = "Blend:Flask")
```

fitted.errors

Extract the fitted values for a fitted model

Description

An alias for the generic function [fitted](#). When it is available, the method [fitted.aovlist](#) extracts the fitted values, which is provided in the **dae** package to cover aovlist objects.

Usage

```
## S3 method for class 'errors'
fitted(object, ...)
```

Arguments

object	An object for which the extraction of model fitted values is meaningful.
...	Further arguments passed to or from other methods.

Value

A numeric vector of fitted values.

Warning

See [fitted.aovlist](#) for specific information about fitted values when an Error function is used in the call to the [aov](#) function.

Author(s)

Chris Brien

See Also

[fitted.aovlist](#), [resid.errors](#), [tukey.1df](#) in package **dae**.

Examples

```
## set up data frame for randomized complete block design in Table 4.4 from
## Box, Hunter and Hunter (2005) Statistics for Experimenters. 2nd edn
## New York, Wiley.
RCBDPen.dat <- fac.gen(list(Blend=5, Flask=4))
RCBDPen.dat$Treat <- factor(rep(c("A","B","C","D"), times=5))
RCBDPen.dat$Yield <- c(89,88,97,94,84,77,92,79,81,87,87,
                      85,87,92,89,84,79,81,80,88)

## perform the analysis of variance
RCBDPen.aov <- aov(Yield ~ Blend + Treat + Error(Blend/Flask), RCBDPen.dat)
summary(RCBDPen.aov)

## three equivalent ways of extracting the fitted values
fit <- fitted.aovlist(RCBDPen.aov)
fit <- fitted(RCBDPen.aov, error.term = "Blend:Flask")
fit <- fitted.errors(RCBDPen.aov, error.term = "Blend:Flask")
```

get.daeTolerance

Gets the value of daeTolerance for the package dae

Description

A function that gets the vector of values such that, in **dae** functions, values less than it are considered to be zero.

Usage

```
get.daeTolerance()
```

Value

The vector of two values for daeTolerance, one named `element.tol` that is used for elements of matrices and a second named `element.eigen` that is used for eigenvalues and quantities based on them, such as efficiency factors.

Author(s)

Chris Brien

See Also

[set.daeTolerance](#).

Examples

```
## get daeTolerance.  
get.daeTolerance()
```

harmonic.mean	<i>Calculates the harmonic mean.</i>
---------------	--------------------------------------

Description

A function to calculate the harmonic mean of a set of nonzero numbers.

Usage

```
harmonic.mean(x)
```

Arguments

x An object from whose elements the harmonic mean is to be computed.

Details

All the elements of **x** are tested as being less than **daeTolerance**, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change **daeTolerance**.

Value

A numeric. Returns Inf if **x** contains a value close to zero

Examples

```
y <- c(seq(0.1,1,0.2))  
harmonic.mean(y)
```

interaction.ABC.plot *Plots an interaction plot for three factors*

Description

Plots a function (the mean by default) of the response for the combinations of the three **factors** specified as the `x.factor` (plotted on the x axis of each plot), the `groups.factor` (plotted as separate lines in each plot) and the `trace.factor` (its levels are plotted in different plots). Interaction plots for more than three **factors** can be produced by using `fac.combine` to combine all but two of them into a single **factor** that is specified as the `trace.factor`.

Usage

```
interaction.ABC.plot(response, x.factor, groups.factor,
  trace.factor, data, fun="mean", title="A:B:C Interaction Plot",
  xlab, ylab, key.title, lwd=4, columns=2, ...)
```

Arguments

<code>response</code>	A numeric vector containing the response variable from which a function (the mean by default) is computed for plotting on the y-axis.
<code>x.factor</code>	The factor to be plotted on the x-axis of each plot.
<code>groups.factor</code>	The factor plotted as separate lines in each plot.
<code>trace.factor</code>	The factor for whose levels there are separate plots.
<code>data</code>	A data.frame containing the three factors and the response.
<code>fun</code>	The function to be computed from the response for each combination of the three factors <code>x.factor</code> , <code>groups.factor</code> and <code>trace.factor</code> . By default, the mean is computed for each combination.
<code>title</code>	Title for plot window. By default it is "A:B:C Interaction Plot".
<code>xlab</code>	Label for the x-axis. By default it is the name of the <code>x.factor</code> .
<code>ylab</code>	Label for the y-axis. By default it is the name of the response.
<code>key.title</code>	Label for the key (legend) to the lines in each plot. By default it is the name of the <code>groups.factor</code> .
<code>lwd</code>	The width of the lines. By default it is 4.
<code>columns</code>	The number of columns for arranging the several plots for the levels of the <code>groups.factor</code> . By default it is 2.
<code>...</code>	Other arguments that are passed down to ggplot methods.

Value

An object of class "ggplot", which can be plotted using `print`.

Author(s)

Chris Brien

See Also

`fac.combine` in package **dae**, `interaction.plot`.

Examples

```
## Not run:
## plot for generated data
## use ?ABC.Interact.dat for data set details
data(ABC.Interact.dat)
interaction.ABC.plot(MOE, A, B, C, data=ABC.Interact.dat)

## plot for Example 14.1 from Mead, R. (1990). The Design of Experiments:
## Statistical Principles for Practical Application. Cambridge,
## Cambridge University Press.
## use ?SPLGrass.dat for details
data(SPLGrass.dat)
interaction.ABC.plot(Main.Grass, x.factor=Period,
                     groups.factor=Spring, trace.factor=Summer,
                     data=SPLGrass.dat,
                     title="Effect of Period, Spring and Summer on Main Grass")

## End(Not run)
```

is.allzero

Tests whether all elements are approximately zero

Description

A single-line function that tests whether all elements are zero (approximately).

Usage

```
is.allzero(x)
```

Arguments

x An object whose elements are to be tested.

Details

The mean of the absolute values of the elements of x is tested to determine if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function `set.daeTolerance` can be used to change `daeTolerance`.

Value

A logical.

Author(s)

Chris Brien

Examples

```
## create a vector of 9 zeroes and a one
y <- c(rep(0,9), 1)

## check that vector is only zeroes is FALSE
is.allzero(y)
```

is.projector*Tests whether an object is a valid object of class projector*

Description

Tests whether an object is a valid object of class "projector".

Usage

```
is.projector(object)
```

Arguments

object The [matrix](#) to be made into a projector.

Details

The function `is.projector` tests whether the object consists of a [matrix](#) that is square, symmetric and idempotent. In checking symmetry and idempotency, the equality of the matrix with either its transpose or square is tested. In this, a difference in elements is considered to be zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

TRUE or FALSE depending on whether the object is a valid object of class "projector".

Warning

The degrees of freedom are not checked. [correct.degfree](#) can be used to check them.

Author(s)

Chris Brien

See Also

[projector](#), [correct.degfree](#) in package **dae**.
[projector](#) for further information about this class.

Examples

```
## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## create an object of class projector
proj.m <- projector(m)

## check that it is a valid projector
is.projector(proj.m)
```

mat.ar1	<i>Forms an ar1 correlation matrix</i>
---------	--

Description

Form the correlation [matrix](#) of order order whose correlations follow the ar1 pattern. The [matrix](#) has diagonal elements equal to one and the off-diagonal element in the ith row and jth column equal to ρ^k where $k = |i - j|$.

Usage

```
mat.ar1(order, rho)
```

Arguments

order	The order of the matrix to be formed.
rho	The correlation on the first off-diagonal.

Value

A correlation [matrix](#) whose elements follow an ar1 pattern.

See Also

[mat.I](#), [mat.J](#), [mat.exp](#), [mat.banded](#)

Examples

```
corr <- mat.ar1(order=4, rho=0.4)
```

mat.banded	<i>Form a banded matrix from a vector of values</i>
------------	---

Description

Takes the first value in `x` and places it down the diagonal of the `matrix`. Takes the second value in `x` and places it down the first subdiagonal, both below and above the diagonal of the `matrix`. The third value is placed in the second subdiagonal and so on, until the bands for which there are elements in `x` have been filled. All other elements in the `matrix` will be zero.

Usage

```
mat.banded(x, nrow, ncol)
```

Arguments

<code>x</code>	A <code>numeric</code> containing the values for each band from 1 to the length of <code>x</code> .
<code>nrow</code>	The number of rows in the banded <code>matrix</code> being formed.
<code>ncol</code>	The number of columns in the banded <code>matrix</code> being formed.

Value

An $nrow \times ncol$ `matrix`.

See Also

`matmult`, `mat.ar1`, `mat.exp`, `mat.I`, `mat.J`

Examples

```
m <- mat.banded(c(1,0.6,0.5), 5,5)
m <- mat.banded(c(1,0.6,0.5), 3,4)
m <- mat.banded(c(1,0.6,0.5), 4,3)
```

mat.dirprod	<i>Forms the direct product of two matrices</i>
-------------	---

Description

Form the direct product of the $m \times n$ `matrix` **A** and the $p \times q$ `matrix` **B**. It is also called the Kroneker product and the right direct product. It is defined to be the result of replacing each element of **A**, a_{ij} , with a_{ij} **B**. The result `matrix` is $mp \times nq$.

The method employed uses the `rep` function to form two $mp \times nq$ matrices: (i) the direct product of **A** and **J**, and (ii) the direct product of **J** and **B**, where each **J** is a matrix of ones whose dimensions are those required to produce an $mp \times nq$ matrix. Then the elementwise product of these two matrices is taken to yield the result.

Usage

```
mat.dirprod(A, B)
```

Arguments

A The left-hand [matrix](#) in the product.
 B The right-hand [matrix](#) in the product.

Value

An $mp \times nq$ [matrix](#).

See Also

matmult, [mat.dirprod](#)

Examples

```
col.I <- mat.I(order=4)
row.I <- mat.I(order=28)
V <- mat.dirprod(col.I, row.I)
```

mat.dirsum

Forms the direct sum of a list of matrices

Description

The direct sum is the partitioned matrices whose diagonal submatrices are the matrices from which the direct sum is to be formed and whose off-diagonal submatrices are conformable matrices of zeroes. The resulting [matrix](#) is $m \times n$, where m is the sum of the numbers of rows of the contributing matrices and n is the sum of their numbers of columns.

Usage

```
mat.dirsum(matrices)
```

Arguments

matrices A list, each of whose component is a [matrix](#).

Value

An $m \times n$ [matrix](#).

See Also

[mat.dirprod](#), [matmult](#)

Examples

```
m1 <- matrix(1:4, nrow=2)
m2 <- matrix(11:16, nrow=3)
m3 <- diag(1, nrow=2, ncol=2)
dsum <- mat.dirsum(list(m1, m2, m3))
```

mat.exp

Forms an exponential correlation matrix

Description

Form the correlation [matrix](#) of order equal to the length of coordinates. The [matrix](#) has diagonal elements equal to one and the off-diagonal element in the *i*th row and *j*th column equal to ρ^k where $k = |\text{coordinate}[i] - \text{coordinate}[j]|$.

Usage

```
mat.exp(coordinates, rho)
```

Arguments

`coordinates` The coordinates of points whose correlation [matrix](#) is to be formed.
`rho` The correlation for points a distance of one apart.

Value

A correlation [matrix](#) whose elements depend on the power of the absolute distance apart.

See Also

[mat.I](#), [mat.J](#), [mat.ar1](#), [mat.banded](#)

Examples

```
corr <- mat.exp(coordinates=c(3:6, 9:12, 15:18), rho=0.1)
```

mat.I

Forms a unit matrix

Description

Form the unit or identity [matrix](#) of order `order`.

Usage

```
mat.I(order)
```

Arguments

`order` The order of the [matrix](#) to be formed.

Value

A square [matrix](#) whose diagonal elements are one and its off-diagonal are zero.

See Also

[mat.J](#), [mat.ar1](#)

Examples

```
col.I <- mat.I(order=4)
```

`mat.J`

Forms a square matrix of ones

Description

Form the square [matrix](#) of ones of order `order`.

Usage

```
mat.J(order)
```

Arguments

`order` The order of the [matrix](#) to be formed.

Value

A square [matrix](#) all of whose elements are one.

See Also

[mat.I](#), [mat.ar1](#)

Examples

```
col.J <- mat.J(order=4)
```

`meanop`

computes the projection matrix that produces means

Description

Replaced by [fac.meanop](#).

mpone	<i>Converts the first two levels of a factor into the numeric values -1 and +1</i>
-------	--

Description

Converts the first two levels of a [factor](#) into the numeric values -1 and +1.

Usage

```
mpone(factor)
```

Arguments

factor The [factor](#) to be converted.

Value

A numeric vector.

Warning

If the [factor](#) has more than two levels they will be coerced to numeric values.

Author(s)

Chris Brien

See Also

[mpone](#) in package **dae**, [factor](#), [relevel](#).

Examples

```
## generate all combinations of two two-level factors
mp <- c("-", "+")
Frf3.trt <- fac.gen(list(A = mp, B = mp))

## add factor C, whose levels are the products of the levles of A and B
Frf3.trt$C <- factor(mpone(Frf3.trt$A)*mpone(Frf3.trt$B), labels = mp)
```

no.reps

*Computes the number of replicates for an experiment***Description**

Computes the number of pure replicates required in an experiment to achieve a specified power.

Usage

```
no.reps(multiple=1., df.num=1.,
        df.denom=expression((df.num + 1.) * (r - 1.)), delta=1.,
        sigma=1., alpha=0.05, power=0.8, tol=0.025, print=FALSE)
```

Arguments

multiple	The multiplier, m, which when multiplied by the number of pure replicates of a treatment, r, gives the number of observations rm used in computing means for some, not necessarily proper, subset of the treatment factors; m is the replication arising from other treatment factors. However, for single treatment factor experiments the subset can only be the treatment factor and m = 1.
df.num	The degrees of freedom of the numerator of the F for testing the term involving the treatment factor subset.
df.denom	The degrees of freedom of the denominator of the F for testing the term involving the treatment factor subset.
delta	The true difference between a pair of means for some, not necessarily proper, subset of the treatment factors.
sigma	The population standard deviation.
alpha	The significance level to be used.
power	The minimum power to be achieved.
tol	The maximum difference tolerated between the power required and the power computed in determining the number of replicates.
print	TRUE or FALSE to have or not have a table of power calculation details printed out.

Value

A single numeric value containing the computed number of pure replicates.

Author(s)

Chris Brien

See Also

[power.exp](#) in package **dae**.

Examples

```
## Compute the number of replicates (blocks) required for a randomized
## complete block design with four treatments.
no.reps(multiple = 1, df.num = 3,
        df.denom = expression(df.num * (r - 1)), delta = 5,
        sigma = sqrt(20), print = TRUE)
```

power.exp

*Computes the power for an experiment***Description**

Computes the power for an experiment.

Usage

```
power.exp(rm=5., df.num=1., df.denom=10., delta=1., sigma=1.,
          alpha=0.05, print=FALSE)
```

Arguments

rm	The number of observations used in computing a mean.
df.num	The degrees of freedom of the numerator of the F for testing the term involving the means.
df.denom	The degrees of freedom of the denominator of the F for testing the term involving the means.
delta	The true difference between a pair of means.
sigma	The population standard deviation.
alpha	The significance level to be used.
print	TRUE or FALSE to have or not have a table of power calculation details printed out.

Value

A single numeric value containing the computed power.

Author(s)

Chris Brien

See Also

[no.reps](#) in package **dae**.

Examples

```
## Compute power for a randomized complete block design with four treatments
## and five blocks.
rm <- 5
power.exp(rm = rm, df.num = 3, df.denom = 3 * (rm - 1), delta = 5,
          sigma = sqrt(20), print = TRUE)
```

print.projector	<i>Print projectors</i>
-----------------	-------------------------

Description

Print an object of class "[projector](#)", displaying the matrix and its degrees of freedom (rank).

Usage

```
## S3 method for class 'projector'
print(x, ...)
```

Arguments

x	The object of class " projector " to be printed.
...	Further arguments passed to or from other methods.

Author(s)

Chris Brien

See Also

[print](#), [print.default](#), [show](#).
[projector](#) for further information about this class.

Examples

```
## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## create an object of class projector
proj.m <- projector(m)

## print the object either using the Method function, the generic function or show
print.projector(proj.m)
print(proj.m)
proj.m
```

print.summary.p2canon	<i>Prints the values in an summary.p2canon object</i>
-----------------------	---

Description

Prints a `summary.p2canon` object, which is also a `data.frame`, in a pretty format.

Usage

```
## S3 method for class 'summary.p2canon'
print(x, ...)
```

Arguments

x A summary.p2canon object.
 ... further arguments passed to print.

Value

No value is returned.

See Also

[summary.p2canon](#)

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain projectors using projs.structure
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition and print summary
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
summ <- summary(unit.trt.p2canon)
print(summ)
```

print.summary.pcanon *Prints the values in an [summary.pcanon](#) object*

Description

Prints a summary.pcanon object, which is also a data.frame, in a pretty format.

Usage

```
## S3 method for class 'summary.pcanon'
print(x, ...)
```

Arguments

x A summary.pcanon object.
 ... further arguments passed to print.

Value

No value is returned.

See Also

[summary.pcanon](#)

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain combined decomposition and summarize
unit.trt.canon <- projs.canon(list(unit=~ Block/Unit, trt=~ trt), data = PBIBD2.lay)
summ <- summary(unit.trt.canon, which = c("aeff", "eeff", "order"))
print(summ)
```

proj2.combine

Compute the projection and Residual operators for two, possibly nonorthogonal, projectors

Description

The canonical relationship between a pair of projectors is established by decomposing the range of Q1 into a part that pertains to Q2 and a part that is orthogonal to Q2. It also produces the nonzero canonical efficiency factors for the joint decomposition of Q1 and Q and the corresponding eigenvectors of Q1 (James and Wilkinson, 1971). Q1 and Q2 may be nonorthogonal.

Usage

```
proj2.combine(Q1, Q2)
```

Arguments

Q1 A symmetric projector whose range is to be decomposed.
 Q2 A symmetric projector whose range in Q1 is required.

Details

The nonzero canonical efficiency factors are the nonzero eigenvalues of $Q1 \%*\% Q2 \%*\% Q1$ (James and Wilkinson, 1971). An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

The eigenvectors are the eigenvectors of Q1 corresponding to the nonzero canonical efficiency factors. The eigenvectors for Q2 can be obtained by premultiplying those for Q1 by Q2.

Qres is computed using equation 4.10 from James and Wilkinson (1971) and Qconf is obtained by subtracting Qres from Q1.

Value

A list with the following components:

1. **efficiencies**: a vector containing the nonzero canonical efficiency factors;
2. **eigenvectors**: an $n \times r$ [matrix](#), where n is the order of the projectors and r is the number of nonzero canonical efficiency factors; it contains the eigenvectors of $Q1$ corresponding to the nonzero canonical efficiency factors.
3. **Qconf**: a projector onto the part of the range of $Q1$ with which $Q2$ is confounded;
4. **Qres**: a projector onto the part of the range of $Q1$ that is orthogonal to the range of $Q2$.

Author(s)

Chris Brien

References

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[proj2.eigen](#), [proj2.efficiency](#), [decomp.relate](#) in package **dae**.

[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

## obtain the projection operators for the interblock analysis
PBIBD2.Bops <- proj2.combine(Q.unit[["Block:Unit"]], Q.trt[["trt"]])
Q.B.T <- PBIBD2.Bops$Qconf
Q.B.res <- PBIBD2.Bops$Qres

## demonstrate their orthogonality
is.allzero(Q.B.T %*% Q.B.res)
```

proj2.decomp	<i>A deprecated function</i>
--------------	------------------------------

Description

A deprecated function - see [proj2.eigen](#)

Usage

```
proj2.decomp()
```

Author(s)

Chris Brien

proj2. efficiency	<i>Computes the canonical efficiency factors for the joint decomposition of two projectors</i>
-------------------	--

Description

Computes the canonical efficiency factors for the joint decomposition of two projectors (James and Wilkinson, 1971).

Usage

```
proj2. efficiency(Q1, Q2)
```

Arguments

Q1	An object of class " projector ".
Q2	An object of class " projector ".

Details

The nonzero canonical efficiency factors are the nonzero eigenvalues of $Q1 \%*\% Q2 \%*\% Q1$ (James and Wilkinson, 1971). An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

A vector containing the nonzero canonical efficiency factors.

Author(s)

Chris Brien

References

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[efficiency.criteria](#), [proj2.eigen](#), [proj2.combine](#) in package **dae**, [eigen](#).
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

## save intrablock efficiencies
eff.intra <- proj2.efficiency(Q.unit[["Block"]], Q.trt[["trt"]])
```

proj2.eigen	<i>Canonical efficiency factors and eigenvectors in joint decomposition of two projectors</i>
-------------	---

Description

Computes the canonical efficiency factors for the joint decomposition of two projectors and the eigenvectors corresponding to the first projector (James and Wilkinson, 1971).

Usage

```
proj2.eigen(Q1, Q2)
```

Arguments

Q1	An object of class " projector ".
Q2	An object of class " projector ".

Details

The component efficiencies is a vector containing the nonzero canonical efficiency factors for the joint decomposition of the two projectors. The nonzero canonical efficiency factors are the nonzero eigenvalues of $Q1 \%*\% Q2 \%*\% Q1$ (James and Wilkinson, 1971). An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about $1.5E-08$). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

The component eigenvectors is an $n \times r$ [matrix](#), where n is the order of the projectors and r is the number of nonzero canonical efficiency factors; it contains the eigenvectors of Q1 corresponding to the nonzero canonical efficiency factors. The eigenvectors for Q2 can be obtained by premultiplying those for Q1 by Q2.

Value

A list with components efficiencies and eigenvectors.

Author(s)

Chris Brien

References

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[proj2.efficiency](#), [proj2.combine](#) in package **dae**, [eigen](#).
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

## obtain intra- and inter-block decompositions
decomp.inter <- proj2.eigen(Q.unit[["Block"]], Q.trt[["trt"]])
decomp.intra <- proj2.eigen(Q.unit[["Block:Unit"]], Q.trt[["trt"]])

#extract intrablock efficiencies
decomp.intra$efficiencies
```

proj2.ops

A deprecated function

Description

A deprecated function - see [proj2.combine](#)

Usage

```
proj2.ops()
```

Author(s)

Chris Brien

projector

Create projectors

Description

The class "[projector](#)" is the subclass of the class "[matrix](#)" in which matrices are square, symmetric and idempotent.

The function `projector` tests whether a [matrix](#) satisfies these criteria and if it does creates a "[projector](#)" object, computing the projector's degrees of freedom and adding them to the object.

Usage

```
projector(Q)
```

Arguments

`Q` The [matrix](#) to be made into a projector.

Details

In checking that the [matrix](#) is square, symmetric and idempotent, the equality of the [matrix](#) with either its transpose or square is tested. In this, a difference in elements is considered to be zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

Value

An object of Class "[projector](#)" that consists of a square, summetric, idempotent [matrix](#) and degrees of freedom (rank) of the [matrix](#).

Author(s)

Chris Brien

See Also

[degfree](#), [correct.degfree](#) in package **dae**.

[projector](#) for further information about this class.

Examples

```
## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## create an object of class projector
proj.m <- projector(m)

## check that it is a valid projector
is.projector(proj.m)
```

projector-class	<i>Class projector</i>
-----------------	------------------------

Description

The class "[projector](#)" is the subclass of matrices that are square, symmetric and idempotent.

[is.projector](#) is the membership function for this class.

[degfree](#) is the extractor function for the degrees of freedom and [degfree<-](#) is the replacement function.

[correct.degfree](#) checks whether the stored degrees of freedom are correct.

Objects from the Class

An object of class "[projector](#)" consists of a square, symmetric, idempotent matrix along with its degrees of freedom (rank).

Objects can be created by calls of the form `new("projector", data, nrow, ncol, byrow, dimnames, ...)`.

However, this does not add the degrees of freedom to the object. These can be added using the replacement function [degfree<-](#). Alternatively, the function [projector](#) creates the new object from a [matrix](#), adding its degrees of freedom at the same time.

Slots

.Data: Object of class "matrix"

degfree: Object of class "integer"

Extends

Class "[matrix](#)", from data part. Class "[array](#)", by class "matrix", distance 2. Class "[structure](#)", by class "matrix", distance 3. Class "[vector](#)", by class "matrix", distance 4, with explicit coerce.

Methods

coerce signature(from = "projector", to = "matrix")

print signature(x = "projector")

show signature(object = "projector")

Author(s)

Chris Brien

See Also

[projector](#), [degfree](#), [correct.degfree](#) in package **dae**.

Examples

```
showClass("projector")

## set up a 2 x 2 mean operator that takes the mean of a vector of 2 values
m <- matrix(rep(0.5,4), nrow=2)

## create an object of class projector
proj.m <- projector(m)

## check that it is a valid projector
is.projector(proj.m)

## create a projector based on the matrix m
proj.m <- new("projector", data=m)

## add its degrees of freedom and print the projector
degfree(proj.m) <- proj.m
```

projs.2canon	<i>A canonical analysis of the relationships between two sets of projectors</i>
--------------	---

Description

Computes the canonical efficiency factors for the joint decomposition of two structures or sets of mutually orthogonally projectors (Brien and Bailey, 2009), orthogonalizing projectors in the Q2 list to those earlier in the list of projectors with which they are partially aliased.

Usage

```
projs.2canon(Q1, Q2)
```

Arguments

Q1	A list whose components are objects of class " projector ".
Q2	A list whose components are objects of class " projector ".

Details

Two loops, one nested within the other, are performed. The first cycles over the components of Q1 and the nested loop cycles over the components of Q2. The joint decomposition of the two projectors in each cycle, one from Q1 (say Q1[[i]]) and the other from Q2 (say Q2[[j]]) is obtained using [proj2.eigen](#). In particular, the nonzero canonical efficiency factors for the joint decomposition of the two projectors is obtained. The nonzero canonical efficiency factors are the nonzero eigenvalues of Q1[[i]] %*% Q2[[j]] %*% Q1[[i]] (James and Wilkinson, 1971). An eigenvalue is regarded as zero if it is less than `daeTolerance`, which is initially set to `.Machine$double.eps ^ 0.5` (about 1.5E-08). The function [set.daeTolerance](#) can be used to change `daeTolerance`.

However, a warning occurs if any pair of Q2 projectors (say $Q2[[j]]$ and $Q2[[k]]$) do not have adjusted orthogonality with respect to any Q1 projector (say $Q1[[i]]$), because they are partially aliased. That is, if $Q2[[j]] \%*\% Q1[[i]] \%*\% Q2[[k]]$ is nonzero for any pair of different Q2 projectors and any Q1 projector. When it is nonzero, the projector for the later term in the list of projectors is orthogonalized to the projector that is earlier in the list.

Value

A list of class p2canon. It has a component for each component of Q1. Each of the components for Q1 is a list; its components are one for each component of Q2 and a component Pres. Each of the Q2 components is a list of three components: pairwise, adjusted and Qproj. These components are based on an eigenanalysis of the relationship between the projectors for the parent Q1 and Q2 components. Each pairwise component is based on the nonzero canonical efficiency factors for the joint decomposition of the two parent projectors (see [proj2.eigen](#)). An adjusted component is based on the nonzero canonical efficiency factors for the joint decomposition of the Q1 component and the Q2 component, the latter adjusted for all Q2 projectors that have occurred previously in the list. The Qproj component is the adjusted projector for the parent Q2 component. The pairwise and adjusted components have the following components: efficiencies, aefficiency, mefficiency, sefficiency, efficiency.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[summary.p2canon](#), [efficiencies.p2canon](#), [projs.combine.p2canon](#), [projs.structure](#), [proj2.efficiency](#), [proj2.combine](#), [proj2.eigen](#), in package **dae**, [eigen](#).
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain projectors using projs.structure
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition and summarize
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
summary(unit.trt.p2canon)
```

projs.canon	<i>A canonical analysis of the relationships between two or more sets of projectors</i>
-------------	---

Description

Computes the canonical efficiency factors for the joint decomposition of two or more structures or sets of mutually orthogonally projectors (Brien and Bailey, 2009), orthogonalizing projectors in a set to those earlier in the set of projectors with which they are partially aliased.

Usage

```
projs.canon(formulae, orthogonalize = "differencingfirst",
            omit.projectors = c("p2canon", "combined"), data = NULL, ...)
```

Arguments

formulae	An object of class list whose components are of class formula.
orthogonalize	A string indicating the method for orthogonalizing a projector to those for terms that occurred previously in the formula. Two options are available: <code>differencingfirst</code> ; <code>eigenmethods</code> .
omit.projectors	A character vector of the types of projectors to omit from the returned pcanon object. If <code>p2canon</code> is included in the vector then the projectors in these objects will be replaced with a numeric containing their degrees of freedom. If <code>combined</code> is included in the vector then the projectors for the combined decomposition will be replaced with a numeric containing their degrees of freedom. If none is included in the vector then no projectors will be omitted.
data	A data frame contains the values of the factors and variables that occur in formulae.
...	further arguments passed to terms.

Details

For each formula supplied in `formulae`, the set of projectors is obtained using `projs.structure`; there is one projector for each term in a formula. Then `projs.2canon` is used to perform an analysis of the canonical relationships between two sets of projectors for the first two formulae. If there are further formulae, the relationships between its projectors and the already established decomposition is obtained using `projs.2canon`. The core of the analysis is the determination of eigenvalues of the product of pairs of projectors using the results of James and Wilkinson (1971).

Value

A list of class pcanon. It has as many components as there are formulae. The first component is the joint decomposition of two structures derived from the first two formulae, being the p2canon object produced by `projs.2canon`. Then there is a component for each further formulae that contains the p2canon object obtained by applying `projs.2canon` to the structure for a formula and the already established joint decomposition of the structures for the previous formulae in the formulae. The last component contains the list of the projectors that give the combined canonical decomposition derived from the formulae.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[summary.pcanon](#), [efficiencies.pcanon](#), [projs.2canon](#), [projs.structure](#), [proj2.efficiency](#), [proj2.combine](#), [proj2.eigen](#), in package **dae**, [eigen](#).
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain combined decomposition and summarize
unit.trt.canon <- projs.canon(list(unit=~ Block/Unit, trt=~ trt), data = PBIBD2.lay)
summary(unit.trt.canon, which = c("aeff","eeff","order"))

## Three-phase sensory example from Brien and Payne (1999)
## Not run: data(Sensory3Phase.dat)
Eval.Field.Treat.canon <- projs.canon(list(
                                eval=~ ((Occasions/Intervals/Sittings)*Judges)/Positions,
                                field=~ (Rows*(Squares/Columns))/Halfplots,
                                treats=~ Trellis*Method), data=Sensory3Phase.dat)
summary(Eval.Field.Treat.canon, which.criteria =c("aefficiency", "order"))

## End(Not run)
```

`projs.combine.p2canon` *Extract, from a p2canon object, the projectors that give the combined canonical decomposition*

Description

Extracts, from a p2canon object obtained using [projs.2canon](#), the projectors that give the combined canonical decomposition of two sets of projectors (Brien and Bailey, 2009).

Usage

```
projs.combine.p2canon(object)
```

Arguments

object A list of class p2canon produced by projs.2canon.

Value

A list, each of whose components is a projector in the decomposition.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

See Also

[projs.2canon](#), [proj2.eigen](#), [proj2.combine](#) in package **dae**.
[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## obtain sets of projectors
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
UcombineT <- projs.combine.p2canon(unit.trt.p2canon)
```

projs.structure

orthogonalised projectors for the terms in a formula

Description

Produces a set of mutually orthogonal projectors, one for each term in the formula. These specify a structure, or an orthogonal decomposition of the data space. Firstly, the primary projector $X(X'X)^{-1}X'$, where X is the design matrix for the term, is calculated for each term. Then this projector is made orthogonal to terms aliased with it. Two methods of orthogonalization are available: `differencingfirst` and `eigenmethods`.

Usage

```
projs.structure(formula, orthogonalize = "differencingfirst", data = NULL, ...)
```

Arguments

formula	An object of class formula from which the terms will be obtained.
orthogonalize	A string indicating the method for orthogonalizing a projector to those for terms that occurred previously in the formula. Two options are available: differencingfirst; eigenmethods.
data	A data frame contains the values of the factors and variables that occur in formula.
...	further arguments passed to terms.

Details

In orthogonalizing a projector to others in the set, the differencingfirst method subtracts from a primary projector each orthogonalized projector for a term whose factors/variables are a subset of its factors/variables. This relies on ensuring that all projectors whose factors/variables are a subset of the current projector occur before it in the expanded formula. It is checked that the set of matrices are mutually orthogonal. If they are not then eigenmethods are employed.

The eigenmethods uses equation 4.10 of James and Wilkinson (1971), which involves calculating the canonical efficiency factors for pairs of primary projectors. The latter method is needed when differencing does not result in a set of mutually orthogonal projectors. It can be invoked directly, especially when it is known that differencing will not produce an orthogonal set of projectors.

Value

A list with a component for each term in the formula, the component containing the orthogonalized projector for the term.

Author(s)

Chris Brien

References

James, A. T. and Wilkinson, G. N. (1971) Factorization of the residual operator and canonical decomposition of nonorthogonal factors in the analysis of variance. *Biometrika*, **58**, 279-294.

See Also

[proj2.efficiency](#), [proj2.combine](#), [proj2.eigen](#), [projs.2canon](#) in package **dae**, [eigen](#).

[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
```

```

PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

## manually obtain projectors for units
Q.G <- projector(matrix(1, nrow=24, ncol=24)/24)
Q.B <- projector(fac.meanop(PBIBD2.lay$Block) - Q.G)
Q.BP <- projector(diag(1, nrow=24) - Q.B - Q.G)

## manually obtain projector for trt
Q.T <- projector(fac.meanop(PBIBD2.lay$trt) - Q.G)

##compute intrablock efficiency criteria
effic <- proj2.efficiency(Q.BP, Q.T)
effic
efficiency.criteria(effic)

##obtain projectors using projs.structure
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition and summarize
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
summary(unit.trt.p2canon, which = c("aeff", "eeff", "order"))

```

qqyeffects

Half or full normal plot of Yates effects

Description

Produces a half or full normal plot of the Yates effects from a 2^k factorial experiment.

Usage

```
qqyeffects(aov.obj, error.term="Within", data=NULL, pch=16,
           full=FALSE, ...)
```

Arguments

<code>aov.obj</code>	An aov object or aovlistobject created from a call to aov .
<code>error.term</code>	The term from the Error function from which the Yates effects are estimated. Only required when Error used in call to aov.
<code>data</code>	A data.frame in which the variables specified in the aov.obj will be found. If missing, the variables are searched for in the standard way.
<code>pch</code>	The number of a plotting symbol to be drawn when plotting points (use <code>help(points)</code> for details).
<code>full</code>	whether a full or half normal plot is to be produced. The default is for a half-normal plot; <code>full=TRUE</code> produces a full normal plot.
<code>...</code>	Further graphical parameters may be specified (use <code>help(par)</code> for possibilities.

Details

A half or full normal plot of the Yates effects is produced. You will be able to interactively select effects to be labelled (click reasonably close to the point and on the side where you want the label placed). **Right click on the graph and select Stop when you have finished labelling effects.** A regression line fitted to the unselected effects and constrained to go through the origin is plotted. Also, a list of the labelled effects, if any, are printed to standard output.

Value

Returns, invisibly, a list with components x and y, giving coordinates of the plotted points.

Author(s)

Chris Brien

See Also

[yates.effects](#) in package **dae**, [qqnorm](#).

Examples

```
## analysis of 2^4 factorial experiment from Table 10.6 of Box, Hunter and
## Hunter (1978) Statistics for Experimenters. New York, Wiley.
## use ?Fac4Proc.dat for data set details
data(Fac4Proc.dat)
Fac4Proc.aov <- aov(Conv ~ Catal * Temp * Press * Conc + Error(Runs),
                    Fac4Proc.dat)
qqyeffects(Fac4Proc.aov, error.term="Runs", data=Fac4Proc.dat)
```

resid.errors

Extract the residuals for a fitted model

Description

An alias for the generic function [residuals](#). When it is available, the method [residuals.aovlist](#) extracts residuals, which is provided in the package **dae** to cover aovlist objects.

Usage

```
resid.errors(object, ...)
```

Arguments

object	An object for which the extraction of residuals is meaningful.
...	Further arguments passed to or from other methods.

Value

A numeric vector containing the residuals.

Note

See [residuals.aovlist](#) for specific information about the residuals when an Error function is used in the call to the [aov](#) function.

Author(s)

Chris Brien

See Also

[fitted.errors](#), [residuals.aovlist](#), [tukey.1df](#) in package **dae**.

Examples

```
## set up data frame for randomized complete block design in Table 4.4 from
## Box, Hunter and Hunter (2005) Statistics for Experimenters. 2nd edn
## New York, Wiley.
RCBDPen.dat <- fac.gen(list(Blend=5, Flask=4))
RCBDPen.dat$Treat <- factor(rep(c("A","B","C","D"), times=5))
RCBDPen.dat$Yield <- c(89,88,97,94,84,77,92,79,81,87,87,
                      85,87,92,89,84,79,81,80,88)

## perform the analysis of variance
RCBDPen.aov <- aov(Yield ~ Blend + Treat + Error(Blend/Flask), RCBDPen.dat)
summary(RCBDPen.aov)

## two equivalent ways of extracting the residuals
res <- residuals.aovlist(RCBDPen.aov)
res <- residuals(RCBDPen.aov, error.term = "Blend:Flask")
res <- resid.errors(RCBDPen.aov)
```

residuals.aovlist	<i>Extract the residuals from an aovlist object</i>
-------------------	---

Description

Extracts the residuals from `error.term` or, if `error.term` is not specified, the last `error.term` in the analysis. It is a method for the generic function [residuals](#).

Usage

```
## S3 method for class 'aovlist'
residuals(object, error.term=NULL, ...)
```

Arguments

<code>object</code>	An aovlist object created from a call to aov .
<code>error.term</code>	The term from the Error function for which the residuals are to be extracted. If <code>error.term</code> is NULL the residuals are extracted from the last Error term.
<code>...</code>	Further arguments passed to or from other methods.

Value

A numeric vector containing the residuals.

Author(s)

Chris Brien

See Also

[fitted.errors](#), [resid.errors](#), [tukey.1df](#) in package **dae**.

Examples

```
## set up data frame for randomized complete block design in Table 4.4 from
## Box, Hunter and Hunter (2005) Statistics for Experimenters. 2nd edn
## New York, Wiley.
RCBDPen.dat <- fac.gen(list(Blend=5, Flask=4))
RCBDPen.dat$Treat <- factor(rep(c("A","B","C","D"), times=5))
RCBDPen.dat$Yield <- c(89,88,97,94,84,77,92,79,81,87,87,
                      85,87,92,89,84,79,81,80,88)

## perform the analysis of variance
RCBDPen.aov <- aov(Yield ~ Blend + Treat + Error(Blend/Flask), RCBDPen.dat)
summary(RCBDPen.aov)

## two equivalent ways of extracting the residuals
res <- residuals.aovlist(RCBDPen.aov)
res <- residuals(RCBDPen.aov, error.term = "Blend:Flask")
```

rmvnorm

generates a vector of random values from a multivariate normal distribution

Description

Generates a vector of random values from an n-dimensional multivariate normal distribution whose mean is given by the n-vector mean and variance by the n x n symmetric matrix V. It uses the method described by Ripley (1987, p.98)

Usage

```
rmvnorm(mean, V, method = 'eigenanalysis')
```

Arguments

mean	The mean vector of the multivariate normal distribution from which the random values are to be generated.
V	The variance matrix of the multivariate normal distribution from which the random values are to be generated.
method	The method used to decompose the variance matrix in producing a a matrix to transform the iid standard normal values. The two methods available are 'eigenanalysis' and 'choleski', where only the first letter of each option is obligatory. The default method is eigenanalysis, which is slower but is likely to be more stable than Choleski decomposition.

Details

The method is: a) uses either the eigenvalue or Choleski decomposition of the variance matrix, V , to form the matrix that transforms an iid vector of values to a vector with variance V ; b) generate a vector of length equal to mean of standard normal values; c) premultiply the vector of standard normal values by the transpose of the upper triangular factor and, to the result, add mean.

Value

A [vector](#) of length n , equal to the length of mean.

Author(s)

Chris Brien

References

Ripley, B. D. (1987) *Stochastic simulation*. Wiley, New York.

See Also

[fac.ar1mat](#), [fac.vcmat](#), in package [dae](#), [rnorm](#), and [chol](#).

Examples

```
## set up a two-level factor and a three-level factor, both of length 12
A <- factor(rep(1:2, each=6))
B <- factor(rep(1:3, each=2, times=2))

## generate random values from a multivariate normal for which
##the mean is 20 for all variables and
##the variance matrix has random effects for factor A, ar1 pattern for B and
##residual random variation
mean <- rep(20, 12)
V <- fac.vcmat(A, 5) + fac.ar1mat(B, 0.6) + 2*mat.I(12)
y <- rmvnorm(mean, V)
```

Sensory3Phase.dat

Data for the three-phase sensory evaluation experiment in Brien, C.J. and Payne, R.W. (1999)

Description

The data is from an experiment involved two phases. In the field phase a viticultural experiment was conducted to investigate the differences between 4 types of trellising and 2 methods of pruning. The design was a split-plot design in which the trellis types were assigned to the main plots using two adjacent Youden squares of 3 rows and 4 columns. Each main plot was split into two subplots (or halfplots) and the methods of pruning assigned at random independently to the two halfplots in each main plot. The produce of each halfplot was made into a wine so that there were 24 wines altogether.

The second phase was an evaluation phase in which the produce from the halfplots was evaluated by 6 judges all of whom took part in 24 sittings. In the first 12 sittings the judges evaluated the wines made from the halfplots of one square; the final 12 sittings were to evaluate the wines from the other

square. At each sitting, each judge assessed two glasses of wine from each of the halplots of one of the main plots. The main plots allocated to the judges at each sitting were determined as follows. For the allocation of rows, each occasion was subdivided into 3 intervals of 4 consecutive sittings. During each interval, each judge examined plots from one particular row, these being determined using two 3x3 Latin squares for each occasion, one for judges 1-3 and the other for judges 4-6. At each sitting judges 1-3 examined wines from one particular column and judges 4-6 examined wines from another column. The columns were randomized to the 2 sets of judges x 3 intervals x 4 sittings using duplicates of a balanced incomplete block design for $v=4$ and $k=2$ that were latinized. This balanced incomplete block design consists of three sets of 2 blocks, each set containing the 4 "treatments". For each interval, a different set of 2 blocks was taken and each block assigned to two sittings, but with the columns within the block placed in reverse order in one sitting compared to the other sitting. Thus, in each interval, a judge would evaluate a wine from each of the 4 columns.

The data.frame contains the following factors, in the order give: Occasion, Judges, Interval, Sitings, Position, Squares, Rows, Columns, Halfplot, Trellis, Method. They are followed by the simulated response variable Score.

The scores are ordered so that the factors Occasion, Judges, Interval, Sitings and Position are in standard order; the remaining factors are in randomized order.

Usage

```
data(Sensory3Phase.dat)
```

Format

A data.frame containing 576 observations of 12 variables.

Source

Statlib data sets, <http://lib.stat.cmu.edu/datasets/sensory>.

References

Brien, C.J. and Payne, R.W. (1999) Tiers, structure formulae and the analysis of complicated experiments. *The Statistician*, 48, 41-52.

set.daeTolerance	<i>Sets the values of daeTolerance for the package dae</i>
------------------	--

Description

A function that sets the values such that, in **dae** functions, values less than it are considered to be zero. The values are stored in a vector named daeTolerance in the daeEnv environment. The vector is of length two and, initially, both values are set to $.Machine$double.eps \wedge 0.5$ (about 1.5E-08). One value is named element.tol and is used for elements of matrices; the second is named element.eigen and is used for eigenvalues and quantities based on them, such as efficiency factors.

Usage

```
set.daeTolerance(element.tol=NULL, eigen.tol=NULL)
```

Arguments

<code>element.tol</code>	The value to to which the first element of the <code>daeTolerance</code> vector is to be set. If more than one value is supplied, only the first value is used.
<code>eigen.tol</code>	The value to to which the second element of the <code>daeTolerance</code> vector is to be set. If more than one value is supplied, only the first value is used.

Value

The vector `daeTolerance` is returned invisibly.

Author(s)

Chris Brien

See Also

[get.daeTolerance](#).

Examples

```
## set daeTolerance.  
set.daeTolerance(1E-04, 1E-08)
```

show-methods

Methods for Function show in Package dae

Description

Methods for function show in Package **dae**

Methods

`signature(object = "projector")` Prints the [matrix](#) and its degrees of freedom.

See Also

[projector](#) for further information about this class.

SPLGrass.dat	<i>Data for an experiment to investigate the effects of grazing patterns on pasture composition</i>
--------------	---

Description

The response variable is the percentage area covered by the principal grass (Main.Grass). The design for the experiment is a split-unit design. The main units are arranged in 3 Rows x 3 Columns. Each main unit is split into 2 SubRows x 2 SubColumns.

The factor Period, with levels 3, 9 and 18 days, is assigned to the main units using a 3 x 3 Latin square. The two-level factors Spring and Summer are assigned to split-units using a criss-cross design within each main unit. The levels of each of Spring and Summer are two different grazing patterns in its season.

Usage

```
data(SPLGrass.dat)
```

Format

A data.frame containing 36 observations of 8 variables.

Source

Example 14.1 from Mead, R. (1990). *The Design of Experiments: Statistical Principles for Practical Application*. Cambridge, Cambridge University Press.

strength	<i>Generate paper strength values</i>
----------	---------------------------------------

Description

Generates paper strength values for an experiment with different temperatures.

Usage

```
strength(nodays, noruns, temperature, ident)
```

Arguments

nodays	The number of days over which the experiment is to be run.
noruns	The number of runs to be performed on each day of the experiment.
temperature	A factor that encapsulates the layout by giving the temperature to be investigated for each run on each day. These must be ordered so that the temperatures for the first day are given in the order in which they are to be investigated on that day. These must be followed by the noruns temperatures for the second day and so on. Consequently, the factor temperature will have nodays*noruns values.
ident	The digits of your student identity number. That is, leave out any letters.

Value

A data.frame object containing the factors day, run and temperature and a vector of the generated strengths.

Author(s)

Chris Brien

Examples

```
## Here temperature is a factor with 4*3 = 12 values whose
## first 3 values specify the temperatures to be applied in
## the 3 runs on the first day, values 4 to 6 specify the
## temperatures for the 3 runs on day 2, and so on.
temperature <- factor(rep(c(80,85,90), 4))
exp.strength <- strength(nodays = 4, noruns = 3,
                        temperature = temperature, ident = 0123456)

## In this second example, a completely randomized design is generated
## for the same 3 temperatures replicated 4 times. The layout is stored
## in the data.frame called Design.
Design <- fac.layout(unrandomized=list(runs = 12),
                    randomized = temperature,
                    seed = 5847123)
## eradicate the unrandomized version of temperature
remove("temperature")

## The 12 temperatures in Design are to be regarded as being assigned to
## days and runs in the same manner as for the first example.
exp.strength <- strength(nodays = 4, noruns = 3,
                        temperature = Design$temperature, ident = 0123456)
```

summary.p2canon

A summary of the results of a canonical analysis of the relationships between two sets of projectors

Description

Produces a summary of the efficiency criteria computed from the canonical efficiency factors for the joint decomposition of two sets of projectors (Brien and Bailey, 2009) obtained using [projs.2canon](#).

Usage

```
## S3 method for class 'p2canon'
summary(object, which.criteria = c("aefficiency", "eefficiency"), ...)
```

Arguments

object	A list of class p2canon produced by projs.2canon.
which.criteria	A character vector nominating the efficiency criteria to be included in the summary. It can be none, all or some combination of aefficiency, mefficiency, eefficiency, sefficiency and order.
...	further arguments affecting the summary produced.

Value

An object of classes `summary.p2canon` and `data.frame`, whose rows correspond to the pairs of projectors, one from the Q1 argument and the other from the Q2 argument from [projs.2canon](#); only pairs with non-zero efficiency factors are included. In addition, a line is included for each nonzero Residual Q1 projector.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

See Also

[projs.2canon](#), [proj2.efficiency](#), [efficiency.criteria](#), [proj2.combine](#), [proj2.eigen](#), [projs.structure](#), [print.summary.p2canon](#) in package **dae**, **eigen**.

[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain projectors using projs.structure
Q.unit <- projs.structure(~ Block/Unit, data = PBIBD2.lay)
Q.trt <- projs.structure(~ trt, data = PBIBD2.lay)

##obtain combined decomposition and summarize
unit.trt.p2canon <- projs.2canon(Q.unit, Q.trt)
summary(unit.trt.p2canon)
```

summary.pcanon

A summary of the results of a canonical analysis of the relationships between two or more sets of projectors

Description

Produces a summary of the efficiency criteria computed from the canonical efficiency factors for the joint decomposition of two or more sets of projectors (Brien and Bailey, 2009) obtained using [projs.canon](#).

Usage

```
## S3 method for class 'pcanon'
summary(object, which.criteria = c("aefficiency", "eefficiency"), ...)
```

Arguments

object A list of class pcanon produced by `projs.canon`.

which.criteria A character vector nominating the efficiency criteria to be included in the summary. It can be none, all or some combination of `aefficiency`, `mefficiency`, `eefficiency`, `sefficiency` and `order`.

... further arguments affecting the summary produced.

Value

An object of classes `summary.pcanon` and `data.frame`, whose rows correspond to subspaces in the decomposition; it is of the nature of a skeleton analysis of variance table. It has an attribute named `ntiers` that is equal to the number of tiers.

Author(s)

Chris Brien

References

Brien, C. J. and R. A. Bailey (2009). Decomposition tables for multitiered experiments. I. A chain of randomizations. *The Annals of Statistics*, **36**, 4184 - 4213.

See Also

[projs.canon](#), [proj2.efficiency](#), [efficiency.criteria](#), [proj2.combine](#), [proj2.eigen](#), [projs.structure](#), [print.summary.pcanon](#) in package **dae**, [eigen](#).

[projector](#) for further information about this class.

Examples

```
## PBIBD(2) from p. 379 of Cochran and Cox (1957) Experimental Designs.
## 2nd edn Wiley, New York
PBIBD2.unit <- list(Block = 6, Unit = 4)
PBIBD2.nest <- list(Unit = "Block")
trt <- factor(c(1,4,2,5, 2,5,3,6, 3,6,1,4, 4,1,5,2, 5,2,6,3, 6,3,4,1))
PBIBD2.lay <- fac.layout(unrandomized = PBIBD2.unit,
                        nested.factors=PBIBD2.nest,
                        randomized = trt)

##obtain combined decomposition and summarize
unit.trt.canon <- projs.canon(list(unit=~ Block/Unit, trt=~ trt), data = PBIBD2.lay)
summary(unit.trt.canon, which = c("aeff", "eeff", "order"))
```

tukey.1df

*Performs Tukey's one-degree-of-freedom-test-for-nonadditivity***Description**

Performs Tukey's one-degree-of-freedom-test-for-nonadditivity on a set of residuals from an analysis of variance.

Usage

```
tukey.1df(aov.obj, data, error.term="Within")
```

Arguments

aov.obj	An aov object or aovlist object created from a call to aov .
error.term	The term from the Error function whose residuals are to be tested for nonadditivity. Only required when the Error function used in call to aov, so that an aovlist object is created.
data	A data.frame containing the original response variable and factors used in the call to aov .

Value

A list containing Tukey.SS, Tukey.F, Tukey.p, Devn.SS_q being the SS_q for the 1df test, F value for test and the p-value for the test.

Note

In computing the test quantities fitted values must be obtained. If `error.term` is specified, fitted values will be the sum of effects extracted from terms from the Error function, but only down to that specified by `error.term`. The order of terms is as given in the ANOVA table. If `error.term` is unspecified, all effects for terms external to any Error terms are extracted and summed.

Extracted effects will only be for terms external to any Error function. If you want effects for terms in the Error function to be included, put them both inside and outside the Error function so they are occur twice.

Author(s)

Chris Brien

See Also

[fitted.errors](#), [resid.errors](#) in package **dae**.

Examples

```
## set up data frame for randomized complete block design in Table 4.4 from
## Box, Hunter and Hunter (2005) Statistics for Experimenters. 2nd edn
## New York, Wiley.
RCBDPen.dat <- fac.gen(list(Blend=5, Flask=4))
RCBDPen.dat$Treat <- factor(rep(c("A", "B", "C", "D"), times=5))
RCBDPen.dat$Yield <- c(89, 88, 97, 94, 84, 77, 92, 79, 81, 87, 87,
```



```

85,87,92,89,84,79,81,80,88)

## perform the analysis of variance
RCBDPen.aov <- aov(Yield ~ Blend + Treat + Error(Blend/Flask), RCBDPen.dat)
summary(RCBDPen.aov)

## Obtain the quantities for Tukey's test
tukey.1df(RCBDPen.aov, RCBDPen.dat, error.term = "Blend:Flask")

```

yates.effects	<i>Extract Yates effects</i>
---------------	------------------------------

Description

Extracts Yates effects from an aov object or aovlist object.

Usage

```
yates.effects(aov.obj, error.term="Within", data=NULL)
```

Arguments

aov.obj	An aov object or aovlist object created from a call to aov .
error.term	The term from the Error function from which the Yates effects are estimated. Only required when Error used in call to aov.
data	A data.frame in which the variables specified in the aov.obj will be found. If missing, the variables are searched for in the standard way.

Details

Yates effects are specific to 2^k experiments, where Yates effects are conventionally defined as the difference between the upper and lower levels of a factor. We follow the convention used in Box, Hunter and Hunter (1978) for scaling of higher order interactions: all the Yates effects are on the same scale, and represent the average difference due to the interaction between two different levels. Effects are estimated only from the error term supplied to the error.term argument.

Value

A vector of the Yates effects.

Author(s)

Chris Brien

See Also

[qqyeffects](#) in package **dae**, [aov](#).

Examples

```
## analysis of 2^4 factorial experiment from Table 10.6 of Box, Hunter and
## Hunter (1978) Statistics for Experimenters. New York, Wiley.
## use ?Fac4Proc.dat for data set details
data(Fac4Proc.dat)
Fac4Proc.aov <- aov(Conv ~ Catal * Temp * Press * Conc + Error(Runs),
                    Fac4Proc.dat)
round(yates.effects(Fac4Proc.aov, error.term="Runs", data=Fac4Proc.dat), 2)
```

Index

*Topic **aplot**

interaction.ABC.plot, 35

*Topic **array**

correct.degfree, 8

decomp.relate, 9

degfree, 11

efficiencies.p2canon, 14

efficiencies.pcanon, 15

efficiency.criteria, 16

elements, 17

fac.ar1mat, 19

fac.meanop, 26

fac.sumop, 29

fac.vcmat, 30

is.projector, 37

mat.ar1, 38

mat.banded, 39

mat.dirprod, 39

mat.dirsum, 40

mat.exp, 41

mat.I, 41

mat.J, 42

print.projector, 46

proj2.combine, 48

proj2.decomp, 50

proj2.efficiency, 50

proj2.eigen, 51

proj2.ops, 52

projector, 53

projector-class, 54

projs.2canon, 55

projs.canon, 57

projs.combine.p2canon, 58

projs.structure, 59

show-methods, 67

summary.p2canon, 69

summary.pcanon, 70

*Topic **classes**

projector-class, 54

*Topic **datagen**

fac.gen, 22

fac.layout, 23

rmvnorm, 64

strength, 68

*Topic **datasets**

ABC.Interact.dat, 6

Fac4Proc.dat, 31

Sensory3Phase.dat, 65

SPLGrass.dat, 68

*Topic **design**

blockboundary.plot, 7

decomp.relate, 9

design.plot, 12

efficiencies.p2canon, 14

efficiencies.pcanon, 15

efficiency.criteria, 16

fac.gen, 22

fac.layout, 23

fac.match, 25

interaction.ABC.plot, 35

no.reps, 44

power.exp, 45

print.summary.p2canon, 46

print.summary.pcanon, 47

proj2.combine, 48

proj2.decomp, 50

proj2.efficiency, 50

proj2.eigen, 51

proj2.ops, 52

projs.2canon, 55

projs.canon, 57

projs.combine.p2canon, 58

projs.structure, 59

qqyeffects, 61

strength, 68

summary.p2canon, 69

summary.pcanon, 70

yates.effects, 73

*Topic **factor**

as.numfac, 6

fac.combine, 20

fac.divide, 21

fac.gen, 22

fac.layout, 23

fac.match, 25

fac.nested, 27

- fac.recode, 28
 - mpone, 43
- *Topic **hplot**
 - interaction.ABC.plot, 35
 - qqyeffects, 61
- *Topic **htest**
 - fitted.aovlist, 31
 - fitted.errors, 32
 - qqyeffects, 61
 - resid.errors, 62
 - residuals.aovlist, 63
 - tukey.1df, 72
 - yates.effects, 73
- *Topic **iplot**
 - qqyeffects, 61
- *Topic **manip**
 - as.numfac, 6
 - elements, 17
 - extab, 18
 - fac.combine, 20
 - fac.divide, 21
 - fac.nested, 27
 - fac.recode, 28
 - get.daeTolerance, 33
 - harmonic.mean, 34
 - is.allzero, 36
 - mpone, 43
 - set.daeTolerance, 66
- *Topic **methods**
 - fitted.aovlist, 31
 - residuals.aovlist, 63
 - show-methods, 67
- *Topic **models**
 - fitted.aovlist, 31
 - fitted.errors, 32
 - resid.errors, 62
 - residuals.aovlist, 63
 - tukey.1df, 72
- *Topic **package**
 - dae-package, 3
- *Topic **plot**
 - blockboundary.plot, 7
 - design.plot, 12
- *Topic **projector**
 - correct.degfree, 8
 - decomp.relate, 9
 - degfree, 11
 - efficiencies.p2canon, 14
 - efficiencies.pcanon, 15
 - efficiency.criteria, 16
 - fac.meanop, 26
 - fac.sumop, 29
 - get.daeTolerance, 33
 - is.projector, 37
 - print.projector, 46
 - print.summary.p2canon, 46
 - print.summary.pcanon, 47
 - proj2.combine, 48
 - proj2.decomp, 50
 - proj2.efficiency, 50
 - proj2.eigen, 51
 - proj2.ops, 52
 - projector, 53
 - projector-class, 54
 - projs.2canon, 55
 - projs.canon, 57
 - projs.combine.p2canon, 58
 - projs.structure, 59
 - set.daeTolerance, 66
 - show-methods, 67
 - summary.p2canon, 69
 - summary.pcanon, 70
- ABC.Interact.dat, 6
- aov, 31, 33, 61, 63, 72, 73
- array, 54
- as.numeric, 6, 7
- as.numfac, 6, 29
- blockboundary.plot, 7, 13
- chol, 65
- coerce, projector, matrix-method
(projector-class), 54
- coerce<-, projector, matrix-method
(projector-class), 54
- correct.degfree, 8, 11, 27, 37, 53–55
- dae (dae-package), 3
- dae-package, 3
- data.frame, 21, 23, 24, 35
- decomp.relate, 9, 49
- degfree, 9, 11, 27, 53–55
- degfree<- (degfree), 11
- design.plot, 7, 8, 12
- efficiencies.p2canon, 14, 56
- efficiencies.pcanon, 15, 58
- efficiency.criteria, 16, 51, 70, 71
- eigen, 10, 14–16, 51, 52, 56, 58, 60, 70, 71
- elements, 17
- extab, 18
- fac.ar1mat, 19, 30, 65
- fac.combine, 20, 22, 23, 27, 29, 30, 35
- fac.divide, 21, 21

- fac.gen, [22](#), [24](#), [28](#)
- fac.layout, [23](#)
- fac.match, [25](#)
- fac.meanop, [20](#), [26](#), [30](#), [42](#)
- fac.nested, [27](#)
- fac.recode, [6](#), [7](#), [28](#)
- fac.sumop, [20](#), [27](#), [29](#), [30](#)
- fac.vcmat, [20](#), [30](#), [65](#)
- Fac4Proc.dat, [31](#)
- factor, [6](#), [7](#), [18–24](#), [26–30](#), [35](#), [43](#), [68](#)
- fitted, [31](#), [32](#)
- fitted(fitted.aovlist), [31](#)
- fitted.aovlist, [31](#), [32](#), [33](#)
- fitted.errors, [32](#), [32](#), [63](#), [64](#), [72](#)

- get.daeTolerance, [33](#), [67](#)
- ggplot, [35](#)

- harmonic.mean, [34](#)

- interaction.ABC.plot, [35](#)
- interaction.plot, [35](#)
- is.allzero, [36](#)
- is.projector, [37](#), [54](#)

- list, [10](#), [20–22](#), [24](#)

- mat.ar1, [38](#), [39](#), [41](#), [42](#)
- mat.banded, [38](#), [39](#), [41](#)
- mat.dirprod, [39](#), [40](#)
- mat.dirsum, [40](#)
- mat.exp, [38](#), [39](#), [41](#)
- mat.I, [38](#), [39](#), [41](#), [41](#), [42](#)
- mat.J, [38](#), [39](#), [41](#), [42](#), [42](#)
- match, [26](#)
- matrix, [7](#), [10](#), [12](#), [13](#), [19](#), [30](#), [37–42](#), [49](#), [52–54](#), [67](#)
- meanop, [42](#)
- mpone, [29](#), [43](#), [43](#)

- no.reps, [44](#), [45](#)
- numeric, [39](#)

- par, [8](#), [13](#)
- polygon, [13](#)
- power.exp, [44](#), [45](#)
- print, [46](#)
- print,projector-method
(print.projector), [46](#)
- print.default, [46](#)
- print.projector, [46](#)
- print.summary.p2canon, [46](#), [70](#)
- print.summary.pcanon, [47](#), [71](#)

- proj2.combine, [10](#), [14–16](#), [48](#), [51](#), [52](#), [56](#), [58–60](#), [70](#), [71](#)
- proj2.decomp, [50](#)
- proj2.efficiency, [14–16](#), [49](#), [50](#), [52](#), [56](#), [58](#), [60](#), [70](#), [71](#)
- proj2.eigen, [9](#), [10](#), [14–16](#), [49–51](#), [51](#), [55](#), [56](#), [58–60](#), [70](#), [71](#)
- proj2.ops, [52](#)
- projector, [8](#), [9](#), [11](#), [14–16](#), [27](#), [37](#), [46](#), [49–53](#), [53](#), [54–56](#), [58–60](#), [67](#), [70](#), [71](#)
- projector-class, [54](#)
- projs.2canon, [14](#), [55](#), [57–60](#), [69](#), [70](#)
- projs.canon, [15](#), [57](#), [70](#), [71](#)
- projs.combine.p2canon, [56](#), [58](#)
- projs.structure, [14](#), [15](#), [56–58](#), [59](#), [70](#), [71](#)

- qqnorm, [62](#)
- qqyeffects, [61](#), [73](#)

- relevel, [29](#), [43](#)
- resid.errors, [32](#), [33](#), [62](#), [64](#), [72](#)
- residuals, [62](#), [63](#)
- residuals(residuals.aovlist), [63](#)
- residuals.aovlist, [62](#), [63](#), [63](#)
- rmvnorm, [64](#)
- rnorm, [65](#)

- Sensory3Phase.dat, [65](#)
- set.daeTolerance, [9–11](#), [34](#), [36](#), [37](#), [48](#), [50](#), [51](#), [53](#), [55](#), [66](#)
- show, [46](#)
- show,ANY-method (show-methods), [67](#)
- show,classRepresentation-method
(show-methods), [67](#)
- show,genericFunction-method
(show-methods), [67](#)
- show,MethodDefinition-method
(show-methods), [67](#)
- show,MethodSelectionReport-method
(show-methods), [67](#)
- show,MethodWithNext-method
(show-methods), [67](#)
- show,ObjectsWithPackage-method
(show-methods), [67](#)
- show,oldClass-method (show-methods), [67](#)
- show,projector-method (show-methods), [67](#)
- show,signature-method (show-methods), [67](#)
- show,traceable-method (show-methods), [67](#)
- show-methods, [67](#)
- SPLGrass.dat, [68](#)
- strength, [68](#)
- structure, [54](#)

summary,p2canon-method
 (summary.p2canon), [69](#)
summary,pcanon-method (summary.pcanon),
 [70](#)
summary.p2canon, [14](#), [46](#), [47](#), [56](#), [69](#)
summary.pcanon, [15](#), [47](#), [48](#), [58](#), [70](#)

tukey.1df, [32](#), [33](#), [63](#), [64](#), [72](#)

vector, [26](#), [54](#), [65](#)

yates.effects, [62](#), [73](#)